Calculation Policy 2024

St. John's Nursery and Infant School

Fair Field Junior School

Statement of Intent

The Poppy Academy Trust is committed to improving the life chances of all our children. We will nurture a passion for learning to enable them to thrive in an ever-changing world.

We have shared values across the Trust which we teach explicitly and throughout the curriculum to the children. At our Church school, these values are rooted in our Christian ethos and distinctive Christian character.

This is reflected in all our relationships between staff, children, parents, governors and the local community. It is reflected in how we teach, what and how our pupils learn within and beyond the classroom.

Calculations Policy	
Written by:	Anna Hinton and Grant Kutner
Date:	14.06.26
Approved by:	LGB
Date:	09.07.26
Review frequency:	Every 3 years
Target Audience:	All stakeholders

Our Local Governing Bodies are dedicated to the promotion of high standards of educational achievement. We are committed to eliminating discrimination, advancing equality of opportunity, and fostering good relations between different groups. These factors were considered in the formation and review of this policy and will be adhered to in its implementation and application across the whole school community.

Introduction

This Calculation Policy has been produced in line with the 2014 National Curriculum for Mathematics to ensure consistency and progression in teaching throughout the school that is age appropriate. It aims to introduce children to the processes of calculation through concrete, pictorial and abstract activities. As children begin to understand the underlying ideas, they develop ways of recording to support their thinking and calculation methods, use particular methods that apply to special cases and learn to interpret and use the signs and symbols involved. This policy shows the natural progression that a child should make in their mathematical education. Children should not progress onto the advanced stages of formal written methods until they have a secure conceptual understanding.

Intent

Maths at St. John's Nursery and Infants and Fair Field aims to develop lively, enquiring and resilient minds which are fluent in the fundamentals of mathematics, building upon knowledge and understanding from KS1 throughout KS2. We strive to ensure children feel confident to apply their skills to everyday life and are motivated when reasoning and problem solving.

Our overall aims for when children leave St. John's Nursery and Infants and Fair Field Junior School are:

- we ensure children feel confident to apply their skills to everyday life and understand that maths is all around us and intrinsic to a successful life.
- develop a positive attitude to mathematics as a subject in which all children gain success and pleasure.
- have access to a high quality maths curriculum that is both challenging and enjoyable, and builds upon previous learning.
- be provided with a variety of mathematical opportunities, which will enable them to make relevant connections.
- ensuring children are confident mathematicians who are not afraid to take risks.
- children are confident when reasoning and make appropriate decisions, applying mathematical thinking in order to solve problems.
- develop an ability to express themselves fluently, to talk about the subject with assurance, using correct mathematical language and vocabulary.
- develop mathematical skills and knowledge and recall of basic number facts and the four operations (addition, subtraction, multiplication and division)
- be able to use this knowledge and understanding to carry out calculations mentally
- make use of pictorial representations and informal notes to help record steps and part answers when using mental methods that generate more information than can be kept in their heads
- have an efficient, reliable, compact written method of calculation for each operation that children can apply with confidence when undertaking calculations that they cannot carry out mentally.
- They will do this by always asking themselves: Can I do this in my head? Can I do this in my head using pictorial representations? Do I need to use a pencil and paper procedure of a formal written method?

Implementation

The school uses Herts for Learning 'ESSENTIAL Maths v2.0' as the scheme of work that provides continuity and progression ensuring appropriate pitch and coverage of the curriculum. We continue to modify to match with our school's approach and the needs of our pupils.

This policy is a statement of the aims, principles and strategies for teaching and learning of calculation strategies in Mathematics. It is designed to help teachers and staff at St. John's Nursery and Infant School and Fair Field Junior School ensure that calculation is taught consistently across the school and to aid them in helping children who may need extra support or challenges. This policy is also designed to help parents, carers and other family members support children's learning by providing an explanation of the methods used in our school.

The policy is set out according to the 4 operations, addition, subtraction, multiplication and division; and incorporates fractions for KS2. Within each specific area, there is a progression of skills, knowledge and layout for written methods. The calculation strategies used will reflect this ideology – moving from concrete to pictorial and then abstract recording leading to more formal written methods. The expectations are that teachers follow this to ensure consistency in approach and delivery at the appropriate stage. Mental methods and strategies will work in partnership with these methods. A variety of mental calculation methods are taught and that recall of facts will be taught in school and tested regularly. The progression of mental methods and expectations will comply with the National Curriculum Statements 2014. It is important staff throughout the trust use the correct mathematical language and encourage pupils to do this also, which will help them develop confidence in their mathematical processes and reasoning. This will take place in class discussions as well as through oral and written feedback, next steps and target setting. The basis of our maths calculation policy is that written methods are complementary to mental methods and should not be seen as separate from them.

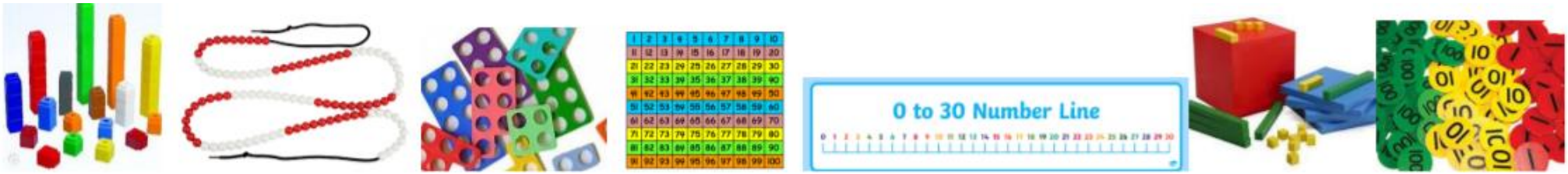
The Importance of Mental Mathematics

While this policy focuses on written calculation in mathematics, we recognise the importance of mental strategies and known facts that form the basis of all calculations. Pupils are provided with frequent opportunities to compare and evaluate different calculation strategies. This helps them develop an understanding that efficiency is personal and based on the numbers involved. Mental maths fluency underpins all effective written calculation approaches.

Concrete, Pictorial and Abstract

Concrete - Manipulatives are objects that can be touched and moved by pupils to introduce, explore or reinforce a mathematical concept. They provide a vehicle to help pupils make sense of complex, symbolic and abstract ideas through exploration and manipulation. Furthermore, they support the development of internal models and help build stronger memory pathways. All pupils should have frequent opportunities to develop their understanding of mathematical concepts through the appropriate use of concrete apparatus.

Concrete resources that may be found in classrooms will include:



These resources will vary depending on year group and individual needs. At home, pupils very well may not have access to these school resources; however, they are just a vehicle to support a pupil's understanding of a topic. Any objects can be used at home to replace counters, cubes etc.
Pictorial (including jottings) - The act of translating the concrete experience into a pictorial representation helps focus attention on what has happened and why. This supports deeper understanding and a stronger imprint on memory. Pictorial representations are more malleable than concrete resources and, once understanding is secured, allow exploration of complex problems that may be challenging to reproduce with manipulatives. When a child is working at the pictorial stage, it often provides rich opportunities for assessment of their depth of understanding.

Abstract - Written The aim, within this policy, is for compacted forms of notation. These have developed through the history of mathematics. Explicit individual steps in procedure are hidden or they have been shortcut. The informal and expanded methods expose all the intermediate steps, replicating thought processes more closely and support understanding prior to compaction.

Abstract - Spoken Learning Our policy is to use the ESSENTIALMATHS speaking frames to develop children's oracy skills, reasoning skills, language structures, and vocabulary. By integrating these frames into our lessons, we support students in articulating their mathematical thinking, fostering clear and confident communication and allowing their ideas to become more permanent. This practice also enhances their ability to construct logical arguments, understand and use complex language structures, and expand their mathematical vocabulary

Impact

Pupils will leave us prepared for the next stage in their lives with:

- Pupils have an appreciation for the maths in everyday life
- Quick recall of facts and procedures
- The flexibility and fluidity to move between different contexts and representations of mathematics
- The ability to recognise relationships and make connections in mathematics
- Confidence and belief that they can achieve
- The knowledge that maths underpins most of our daily lives

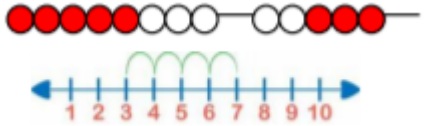
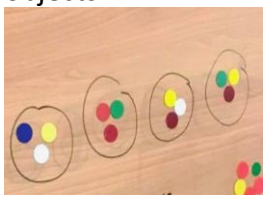
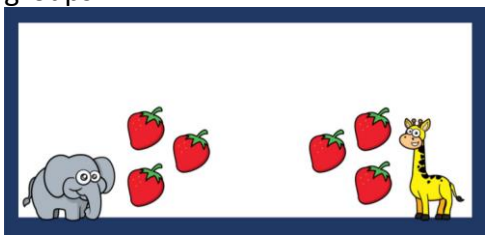
- Skills and concepts that have been mastered
- Have a positive and inquisitive attitude to mathematics as an interesting and attractive subject in which all children gain success and pleasure.

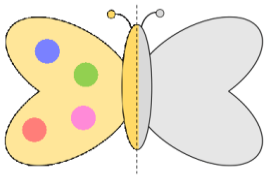
A mathematical concept or skill has been mastered when a child can show it in multiple ways, using the mathematical language to explain their ideas, and can independently apply the concept to new problems in unfamiliar situations. This is the goal for our children. These will be assessed through: assessment, tracking, pupil progress meetings, performance management, moderation and standardisation.

Early Years Foundation Stage

Children at the expected level of development will:

- Have a deep understanding of number to 10, including the composition of each number
- Subitise (recognise quantities without counting) up to 5
- Automatically recall (without reference to rhymes, counting or other aids) number bonds up to 5 (including subtraction facts) and some number bonds to 10, including double facts.

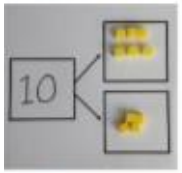
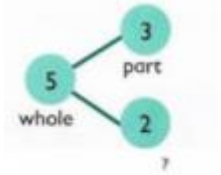
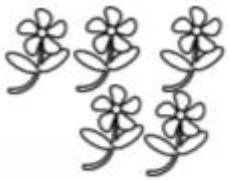
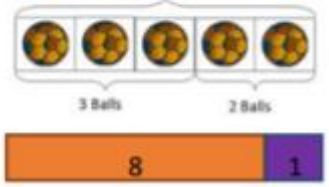
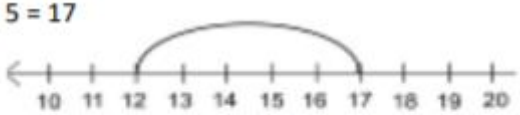
Addition	Subtraction	Multiplication	Division
Children are encouraged to gain a sense of the number system through the use of counting concrete objects.  ways and count all.  They understand addition as counting on and will count on in ones using object s, cubes, bead string and number line.  They use concrete and pictorial representation to record their calculations.	Children are encouraged to gain a sense of the number system through the use of counting concrete objects and understand subtraction as counting out.  They begin to count back in ones using objects, cubes, bead string and number line.  They may use concrete and pictorial representation to record their calculations.	Children use concrete objects to make and count equal groups of objects.  They understand doubling as repeated addition. 4+4 =8	Children use concrete objects to count and share equally into 2 groups.  They count a set of objects and halve them by making two equal groups. .

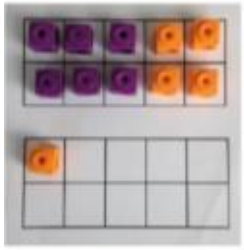
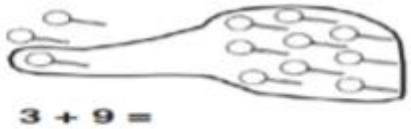
When confident children may be able to pictorially represent their calculations using symbols and numbers within a written	They are encouraged to develop a mental picture of the number system in their heads to use for calculations. When confident children may be able to represent their calculations using symbols and numbers within a written calculation.	 They use concrete and pictorial representation to record their calculations. When confident children may be able to represent their calculations using symbols and numbers within a written calculation. 	 They will begin to use objects to make groups of 2 from a given amount. They use concrete and pictorial representation to record their calculations. 

Year 1 Addition

Pupils should be able to:

- read, write and interpret mathematical statements involving addition (+) and equals (=) signs
- represent and use number bonds and related subtraction facts within 20
- add and subtract one-digit and two-digit numbers to 20, including zero solve one-step problems that involve addition, using concrete objects and pictorial representations, and missing number problems such as 7 = – 9.
- Using speaking frames to develop children's oracy skills, reasoning skills, language structures, and vocabulary.

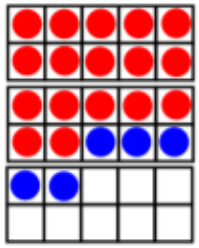
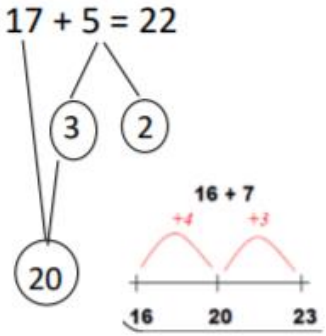
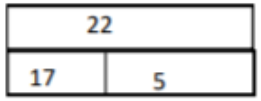
Combining two parts to make a whole: part- whole model	   Use part part whole model. Use cubes to add two numbers together as a group or in a bar. 	   Use pictures to add two numbers together as a group or in a bar.	Part whole model drawing **Speaking Frame -** **Finding Combinations of Coins for Different Values** **The ... rod represents ☐p.** **To make ☐p, you can combine a ☐p coin, ☐p coin ...** **So** **☐p is equal to ☐p and ☐p ...** **☐p = ☐p + ☐p + ...**
Starting with the biggest number and counting on	 Start with the larger number on the bead string and then count on to the smaller number 1 by 1 to find the answer.	12 + 5 = 17  Start at the larger number on the number line and count on in ones or in one jump to find the answer.	Place the larger number in your head and count on the smaller number to find your answer.

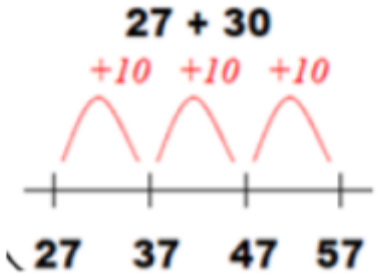
Regrouping to make 10. (This is an essential skill for column addition later).	 6 + 5 = 11  Start with the bigger number and use the smaller number to make 10. Use ten frames.	 3 + 9 = Use pictures or a number line. Regroup or partition the smaller number using the part part whole model to make 10.	7 + 4= 11 If I am at seven, how many more do I need to make 10. How many more do I add on now?

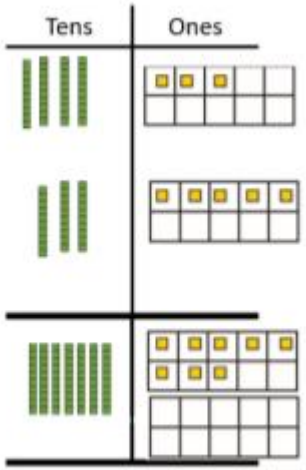
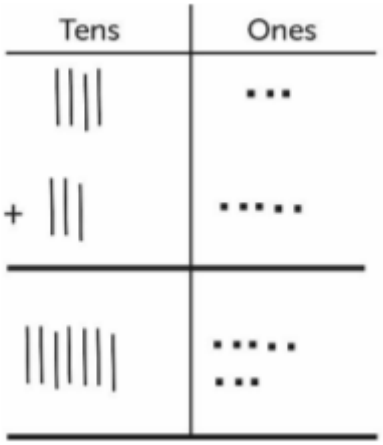
Year 2 Addition

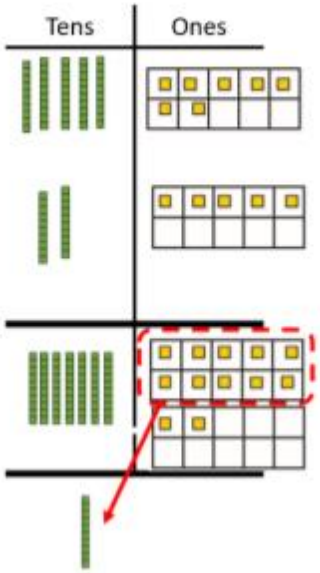
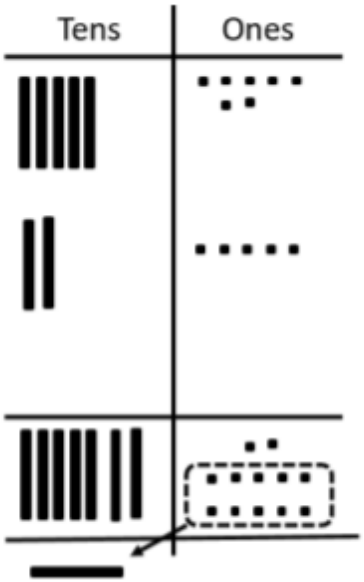
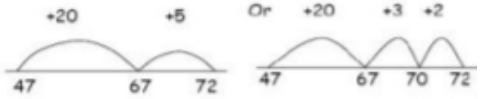
Pupils should be taught to:

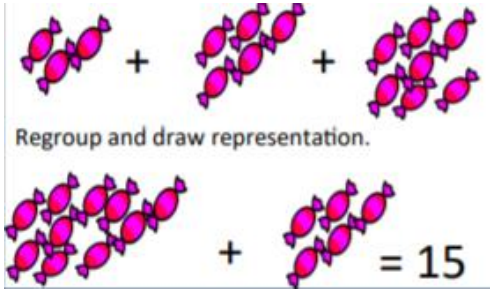
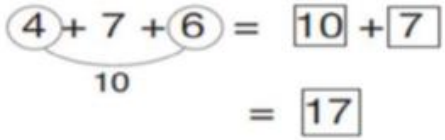
- add numbers using concrete objects, pictorial representations, and mentally including:
  - a two-digit number and ones
  - two two-digit numbers
  - adding three one-digit numbers
- solve problems with addition: using concrete objects and pictorial representations, including those involving numbers, quantities and measures
- applying their increasing knowledge of mental and written methods
- recall and use addition facts to 20 fluently, and derive and use related facts up to 100

Objectives and strategy	Concrete	Pictorial	Abstract
Add a two digit number and ones	 17 + 5 = 22 Use ten frame to make 'magic ten Children explore the pattern. 17 + 5 = 22 27 + 5 = 32	Use part part whole and number line to model. 	17 + 5 = 22 Explore related facts 17 + 5 = 22 5 + 17 = 22 22—17 = 5 22—5 = 17 

Add a 2 digit number and tens	 25 + 10 = 35 Explore that the ones digit does not change		27 + 10 = 37 27 + 20 = 47 27 + □ = 57

Add two 2-digit numbers (without regrouping)	 Using base-ten, numicon and place value counters to support adding two 2-digit numbers without regrouping.	 When confident they will begin to draw the expanded written method. We provide lots of strategies for adding two digit numbers for example number lines -	Adding tens and ones - 40 3 + 30 5 70 8 43 + 35 = 78 When confident they will begin to use the expanded written method to add two digit numbers.

Add two digit numbers with regrouping (through ten)	 Add the ones and regroup them on the tens frame to exchange for a ten. Add the tens together.	 After practically using the base ten, they will begin to draw using a pictorial representation of the expanded written method (with regrouping).  Use number line and bridge ten using part whole if necessary.	When they are confident they will begin to use the expanded written method to add two two -digit numbers with regrouping. 50 + 7 + 20 + 5 70 + ~~12~~ 2 10 57 + 25 = 82 Children will also have the opportunity to use partitioning for addition. 25 + 47 20 + 5 40 + 7 20 + 40 = 60 5+ 7 =12 60 + 12 = 72

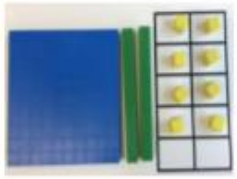
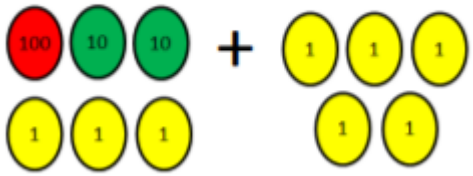
Add three 1-digit numbers.	 Combine to make 10 first if possible, or bridge 1o then add third digit	 Regroup and draw representation. 	 Combine the two numbers that make/ bridge ten then add on the third.

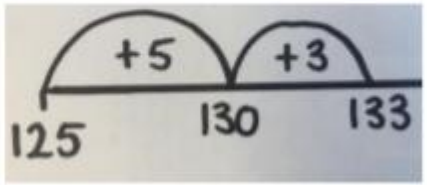
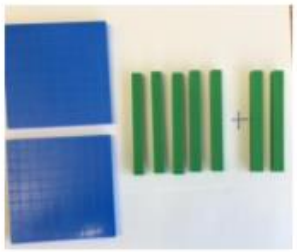
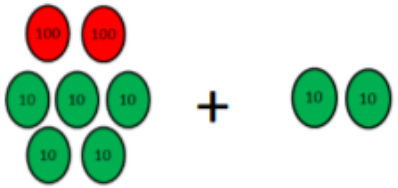
Year 3 - Addition

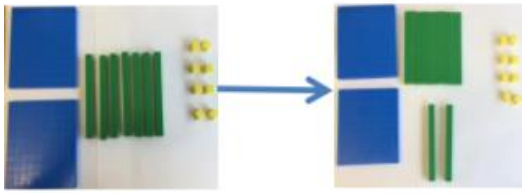
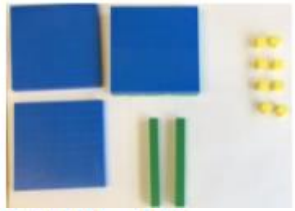
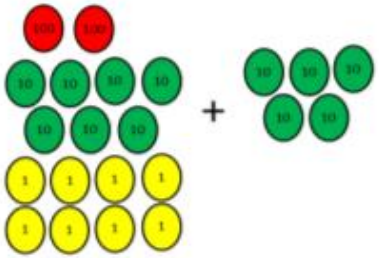
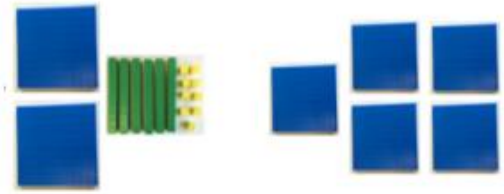
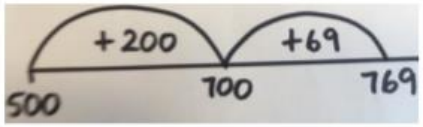
Pupils should be taught to:

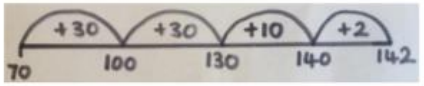
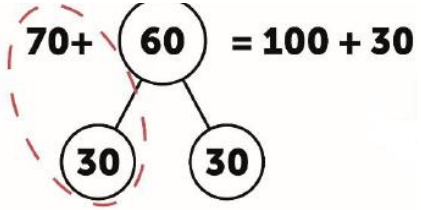
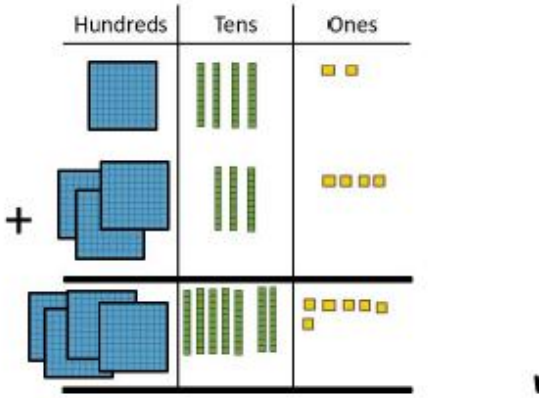
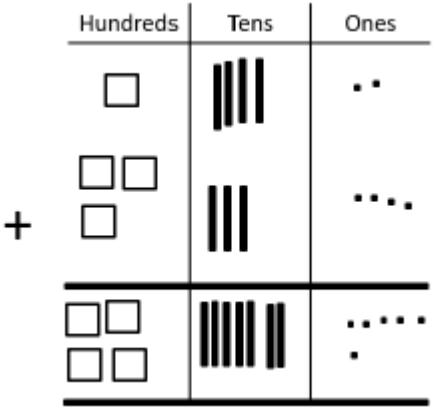
- add numbers mentally, including:
- a three-digit number and 1s
- a three-digit number and 10s
- a three-digit number and 100s
- add numbers with up to 3 digits, using formal written methods of columnar addition
- solve problems, including missing number problems, using number facts, place value, and more complex addition.

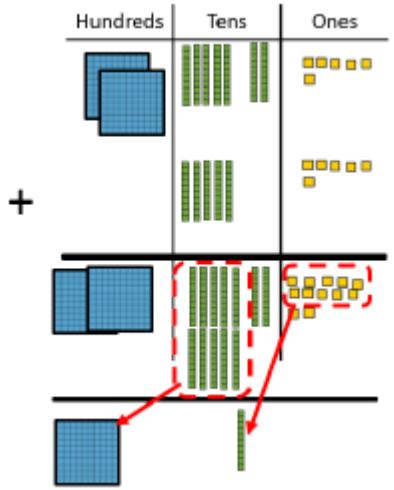
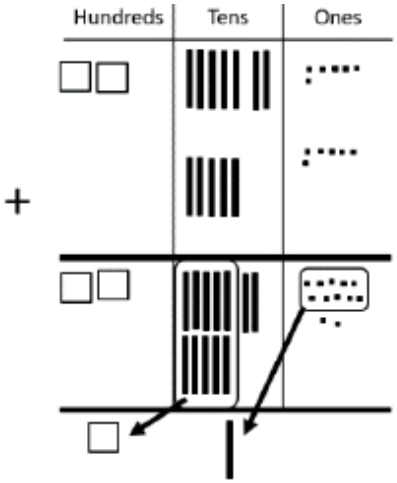
Bar models to be used to support decision making and where the missing numbers fit in our calculations.

Addition of HTO + O without regrouping	**123 + 5 = 128**   	**123 + 5 = 128** 	**123 + 5 = 120 + 8**

Addition of HTO + O with regrouping	**125 + 8 = 133** 	**125 + 8 = 133** 	**125 + 8 = 133** 125 + 5 + 3 = 133
Addition of HTO + T without regrouping	**250 + 20 = 270**  	**250 + 20 = 270** 	**250 + 20 = 200 + 70** *Leading to any HTO + multiple of 10 (not crossing the ten boundary)* **234 + 30 = 200 + 60 + 4**

Addition of HTO + T with regrouping	**278 + 50 = 328**  *Children to understand the exchange of 10 tens for one hundred.* 	**278 + 50 = 328** 	**278 + 50 = 328** 270 + 50 + 8 = 328
Addition of HTO + H	**269 + 500 = 769**  	**269 + 500 = 769** 	**269 + 500 = 769** 200 + 500 + 69 = 769

Addition of any TO + TO Using Partitioning	**79 + 63 = 142**   And the same with place value counters ensuring children understand the exchange.	**79 + 63 = 142** 	**79 + 63 = 142** 70 + 60 = 130 9 + 3 = 9 + 1 + 2 130 + 12 = 142  **100 + 30 = 130**
Add 3 digit numbers together without regrouping			1 4 2 + 3 3 4 4 7 6 142 + 334 = 476

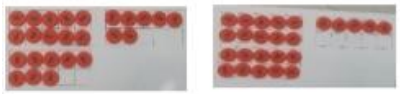
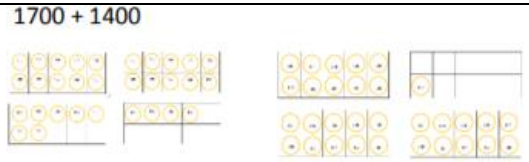
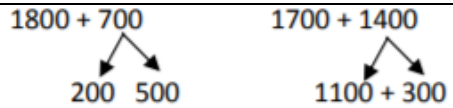
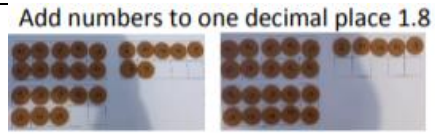
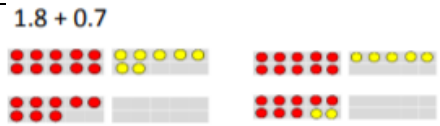
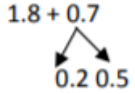
Add 3 digit numbers together with regrouping			2 7 6 + 5 6 3 3 2 1 1 276 + 56 = 332

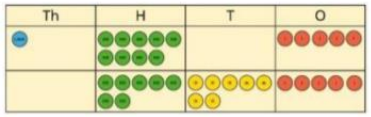
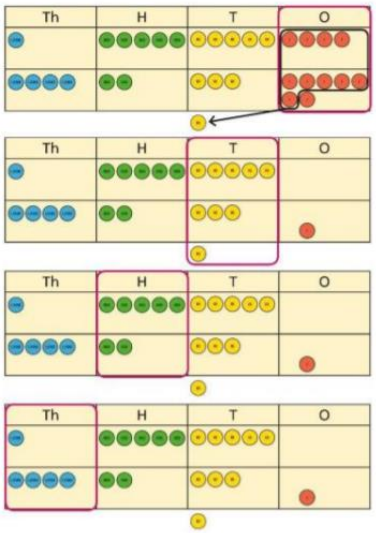
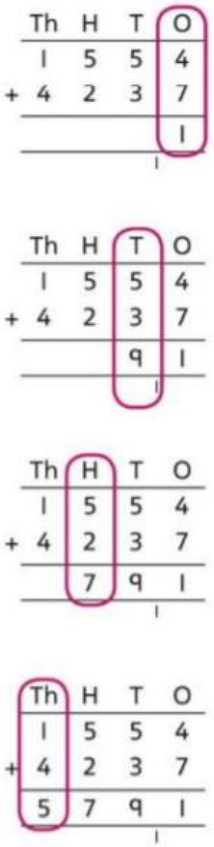
Year 4 - Addition

Pupils should be taught to:

- Add numbers with up to 4 digits using the formal written methods of columnar addition where appropriate
- Estimate and use inverse operations to check answers to a calculation
- Solve addition two-step problems in contexts, deciding which operations and methods to use and why

Bar models to be used to support decision making and where the missing numbers fit in our calculations.

Adding a multiple of 1000 or 100 to a 4 digit number			
Mental calculations (rounding, doubling, using number bonds, adding near doubles)			
Add numbers to one decimal place			

Add numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate.	Use place value equipment on a place value grid to organise thinking. Ensure that children understand how the columns relate to place value and what to do if the numbers are not all 4-digit numbers. *Use equipment.to show 1,905 + 775.*  *Why have only three columns been used for the second row? Why is the Thousands box empty?* *Which columns will total 10 or more?*	Use place value equipment to model required exchanges.  Include examples that exchange in more than one column.	Use a column method to add, including exchanges.  Include examples that exchange in more than one column.

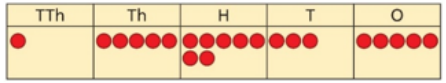
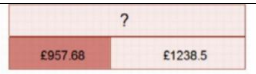
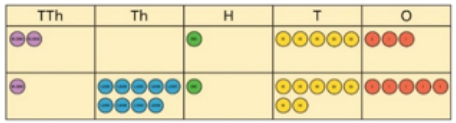
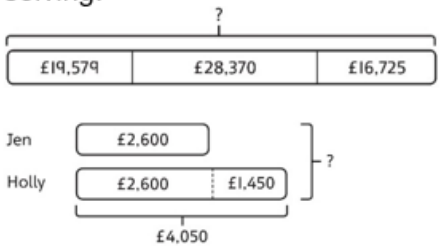
Addition Year 5

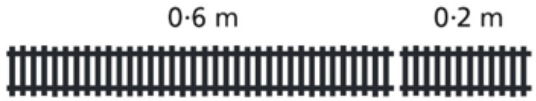
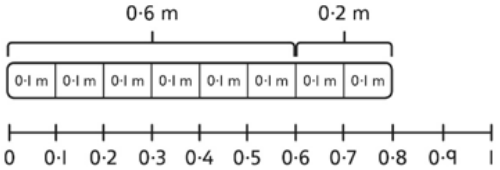
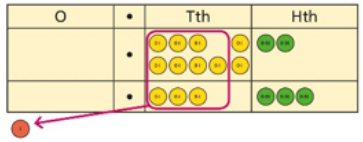
Pupils should be taught to:

- Add whole numbers with more than 4 digits, including using formal written methods (columnar addition)
- Add numbers mentally with increasingly large numbers
- Solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why

Bar models to be used to support decision making and where the missing numbers fit in our calculations.

Mental calculations (rounding, doubling, using number bonds, adding near doubles)		Oracy ☐ is approximately ☐. ☐ is approximately ☐. ☐ - ☐ = ☐ or ☐ + ☐ = ☐ I estimate the answer will be about ☐.	Examples **1445 + 2999** 1445 + 3000 – 1 **1299 + 1299** Double 1300 - 2 **443 + 445** Near double 443 + 2 **12.36 + 5.24** 0.36 + 0.24 = 0.6 17 + 0.6 = 17.6 **36.25 + 23.43** Add each place value column individually

Addition of two numbers (more than 4 digits) using column addition.	Use place value equipment to represent additions. *Add a row of counters onto the place value grid to show 15,735 + 4,012.* 	MacDonalds sold £9957.68 worth of hamburgers and £1238.5 worth of chicken nuggets. How much money did they take altogether?  Represent additions, using place value equipment on a place value grid alongside written methods.  *I need to exchange 10 tens for a 100.* TTh Th H T O 2 0 1 5 3 + 1 9 1 7 5 3 9 3 2 8	Formal method (using carrying) with more than four digits 55825 + 37486 = 93312 (1 1 1) 75879 + 9486 = 85365 (1 1 1 1) Use formal method to solve two-step problems in contexts. 12·73 + 8·39 = 21·12 (1 1 1) £44·73 + £8·39 = £53·12 (1 1 1)
Representing Additions		Bar models represent addition of two or more numbers in the context of problem solving.  Th H T O 2 6 0 0 + 1 4 5 0 4 0 5 0 Th H T O 2 6 0 0 + 4 0 5 0 6 6 5 0	Use approximation to check whether answers are reasonable. TTh Th H T O 2 3 4 0 5 + 7 8 9 2 2 0 2 9 7 TTh Th H T O 2 3 4 0 5 + 7 8 9 2 3 1 2 9 7 *I will use 23,000 + 8,000 to check.*

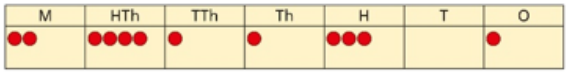
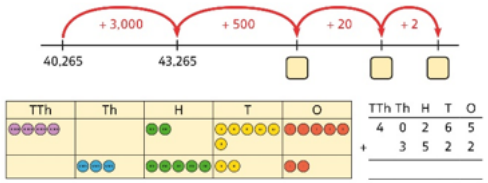
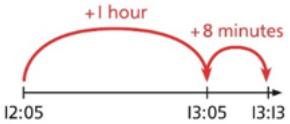
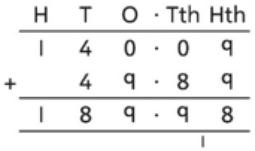
Adding Tenths	Link measure with addition of decimals. *Two lengths of fencing are 0·6 m and 0·2 m.* *How long are they when added together?*  	Use a bar model with a number line to add tenths.  *0·6 + 0·2 = 0·8* *6 tenths + 2 tenths = 8 tenths*	Understand the link with adding fractions. $\frac{6}{10} + \frac{2}{10} = \frac{8}{10}$ *6 tenths + 2 tenths = 8 tenths* *0·6 + 0·2 = 0·8*
Adding decimals using column addition	Use place value equipment to represent additions. *Show 0·23 + 0·45 using place value counters.*	Use place value equipment on a place value grid to represent additions. Represent exchange where necessary.  O · Tth Hth 0 · 9 2 + 0 · 3 3 1 · 2 5 Include examples where the numbers of decimal places are different.  O · Tth Hth 5 · 0 0 + 1 · 2 5 6 · 2 5	Add using a column method, ensuring that children understand the link with place value. O · Tth Hth 0 · 2 3 + 0 · 4 5 0 · 6 8 Include exchange where required, alongside an understanding of place value. O · Tth Hth 0 · 9 2 + 0 · 3 3 1 · 2 5 Include additions where the numbers of decimal places are different. *3.4 + 0.65 = ?* O · Tth Hth 3 · 4 0 + 0 · 6 5

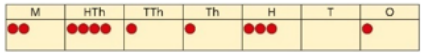
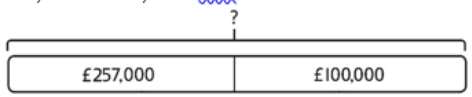
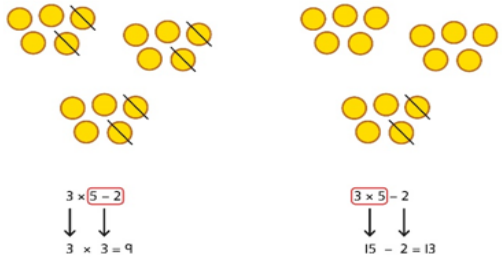
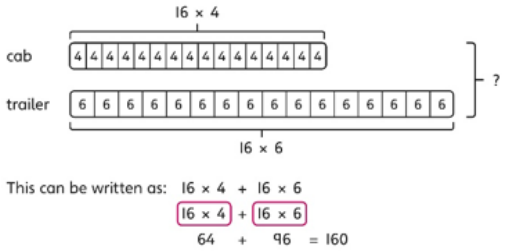
Addition Year 6

Pupils should be taught to:

- perform mental calculations, using increasingly large numbers
- use their knowledge of the order of operations to carry out calculations involving the 4 operations
- solve addition multi-step problems in contexts, deciding which methods to use and why solve problems involving addition

Bar models to be used to support decision making and where the missing numbers fit in our calculations

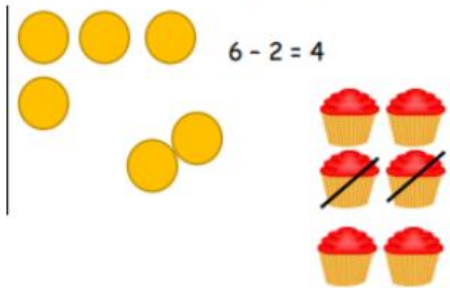
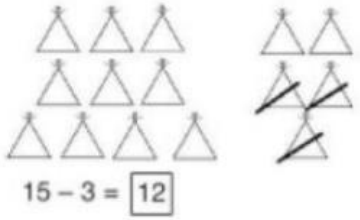
Comparing and selecting efficient methods	Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.  	Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation. Compare written and mental methods alongside place value representations.  Use bar model and number line representations to model addition in problem-solving and measure contexts.  	Use column addition where mental methods are not efficient. Recognise common errors with column addition. *32,145 + 4,302 = ?*  *Which method has been completed accurately?* *What mistake has been made?* Column methods are also used for decimal additions where mental methods are not efficient. 

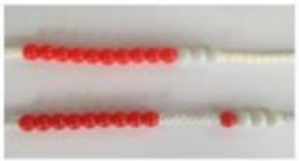
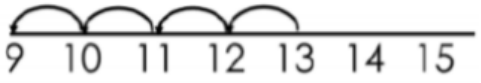
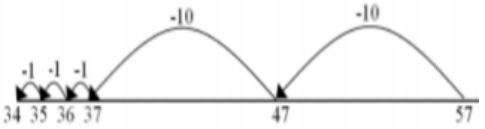
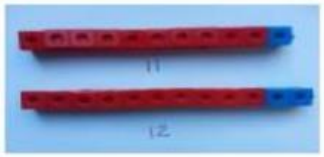
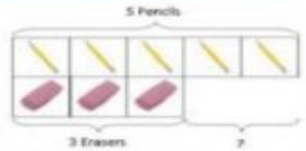
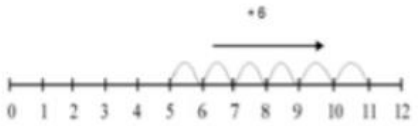
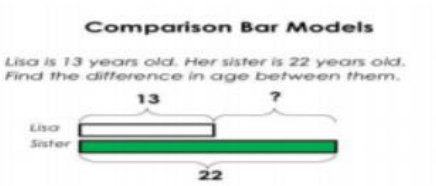
Selecting mental methods for larger numbers where appropriate	Represent 7-digit numbers on a place value grid, and use this to support thinking and mental methods.  *2,411,301 + 500,000 = ?* *This would be 5 more counters in the HTh place.* *So, the total is 2,911,301.* *2,411,301 + 500,000 = 2,911,301*	Use a bar model to support thinking in addition problems. *257,000 + 99,000 = ?*  *I added 100 thousands then subtracted 1 thousand.* *257 thousands + 100 thousands = 357 thousands* *257,000 + 100,000 = 357,000* *357,000 – 1,000 = 356,000* *So, 257,000 + 99,000 = 356,000*	Use place value and unitising to support mental calculations with larger numbers. *195,000 + 6,000 = ?* *195 + 5 + 1 = 201* *195 thousands + 6 thousands = 201 thousands* *So, 195,000 + 6,000 = 201,000*
Understanding order of operations in calculations	Use equipment to model different interpretations of a calculation with more than one operation. Explore different results. *3 × 5 − 2 = ?*  	Model calculations using a bar model to demonstrate the correct order of operations in multi-step calculations.  	Understand the correct order of operations in calculations without brackets. Understand how brackets affect the order of operations in a calculation. *4 + 6 × 16* *4 + 96 = 100* *(4 + 6) × 16* *10 × 16 = 160*

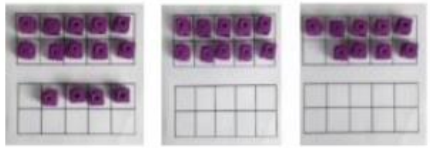
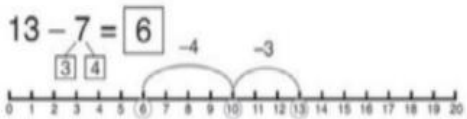
Year 1 Subtraction

Pupils should be taught to:

- read, write and interpret mathematical statements involving addition (+), subtraction (–) and equals (=) signs
- represent and use number bonds and related subtraction facts within 20
- add and subtract one-digit and two-digit numbers to 20, including zero
- solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = – 9.

Taking away ones	Use physical objects, counters, cubes etc. to show how objects can be taken away. 	Cross out drawn objects to show what has been taken away. 	Show subtraction number sentence. **18 - 3 = 15** **8 – 2 = 6**

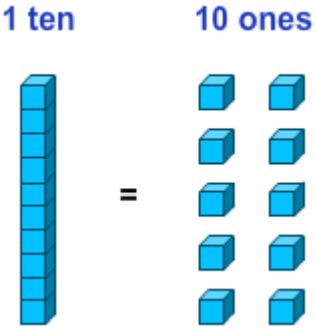
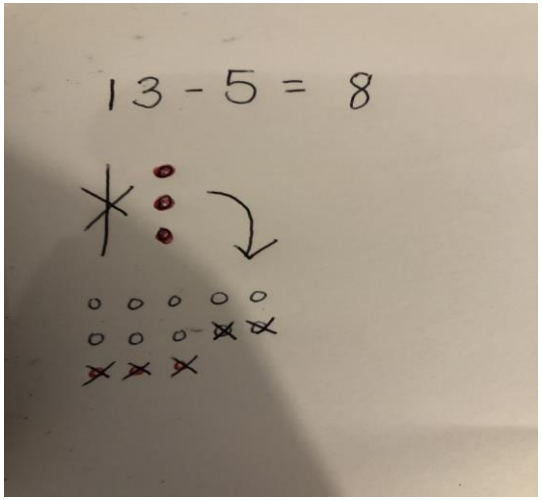
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. **13 – 4 =**  Use counters and move them away from the group as you take them away counting backwards as you go. 	Count back on a number line or number track.  Start at the bigger number and count back the smaller number showing the jumps on the number line.  This can progress all the way to counting back using two 2 digit numbers.	Put 13 in your head, count back 4. What number are you at? Use your fingers to help. **13 - 4 =**
Find the difference	Compare amounts and objects to find the difference.   Use cubes to build towers or make bars to find the difference. Use basic bar models with items to find the difference	Count on to find the difference.  Draw bars to find the difference between 2 numbers.  	Hannah has 23 sandwiches, Helen has 15 sandwiches. Find the difference between the number of sandwiches. **23 - 15 =**

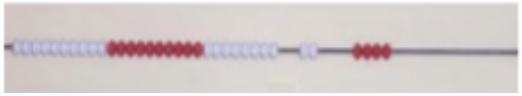
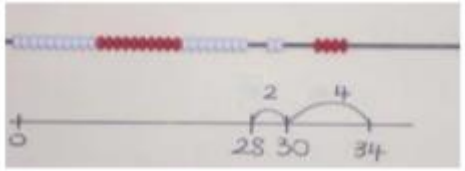
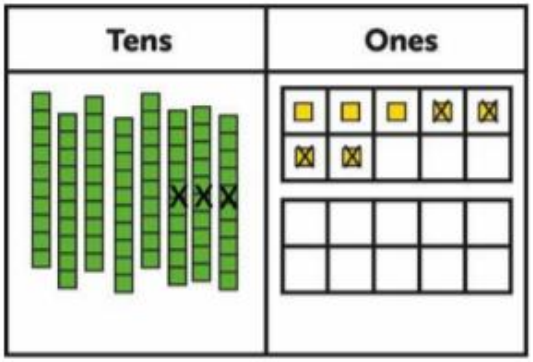
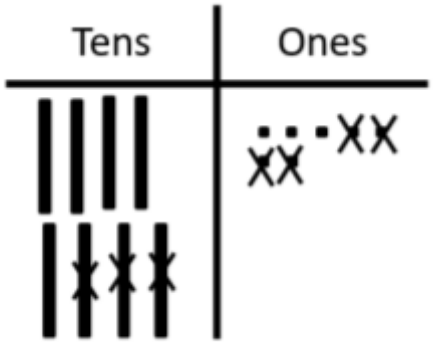
Part Part Whole Model	Make 14 on the ten frame. Take away the four first to make 10 and then takeaway one more so you have taken away 5. You are left with the answer of 9.  14 – 9 =	 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	How many do we take off to reach the next 10? How many do we have left to take off? **16 – 8 =**

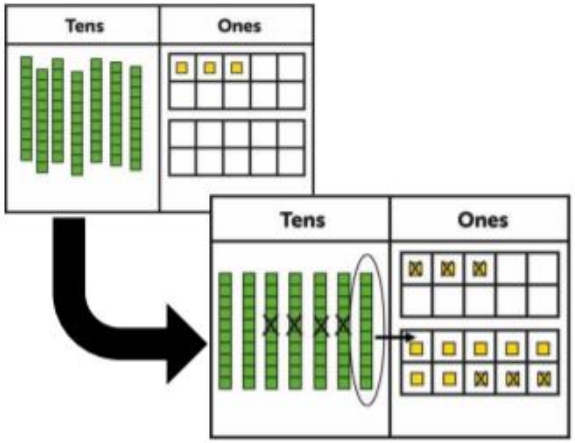
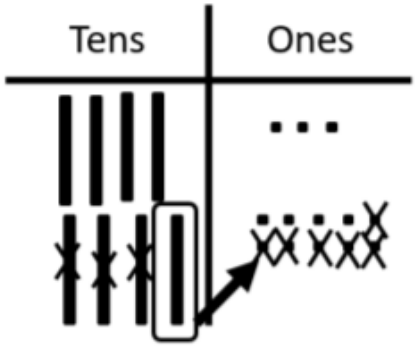
Year 2 Subtraction

Pupils should be able to:

- solve problems with subtraction: using concrete objects and pictorial representations, including those involving numbers, quantities and measures
- applying their increasing knowledge of mental and written methods recall and use subtraction facts to 20 fluently, and derive and use related facts up to 100
- subtract numbers using concrete objects, pictorial representations, and mentally, including:
- a two-digit number and ones
- a two-digit number and tens
- two two-digit numbers

Objectives and strategies	Concrete	Pictorial	Abstract
Regroup a ten into ten ones and subtract.			13 - 5 = 8

Make ten strategy Progression should be crossing one ten, crossing more than one ten, crossing the hundreds.		 34—28 Use a bead bar or bead strings to model counting to next ten and the rest.	
Subtract two two digit numbers without regrouping.	Make the two-digit number using tens and ones and then take away the amount to be subtracted. 87-34 = 53 		When confident, children will begin to use the expanded written method to subtract tens and ones. 80 + 7 - 30 + 4 50 + 3 87 – 34 = 53

Subtract two digit numbers with regrouping.	Make tens and ones and then regroup one ten for ten ones to be able to subtract the number.  	Children will assess if they need to use regrouping to solve the two digit subtraction question. Draw the method they need to use.  	When confident, children will begin to use the expanded written method to subtract tens and ones. 60 13 ~~70~~ ~~3~~ − 40 6 20 □ 7 73 – 46 = 27

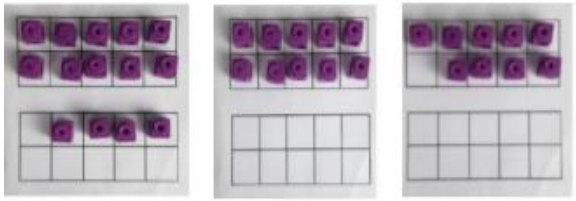
Subtraction Year 3

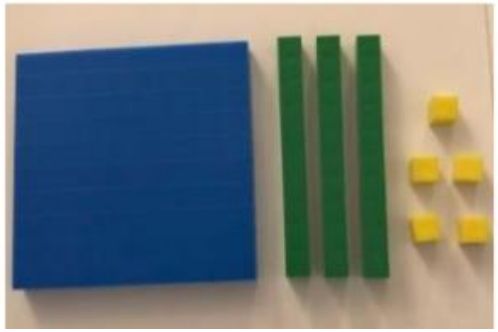
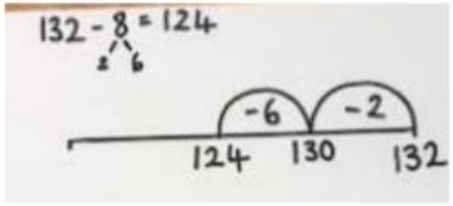
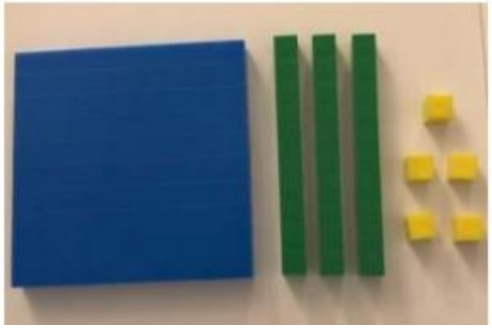
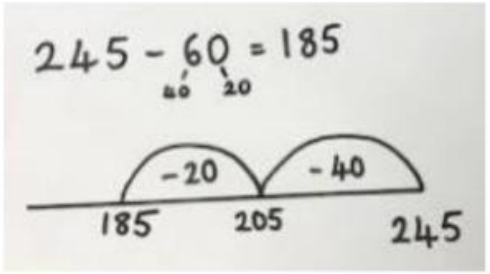
Pupils should be taught to:

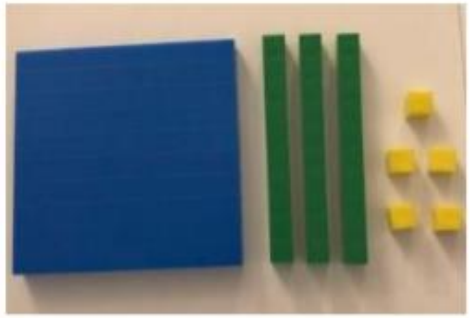
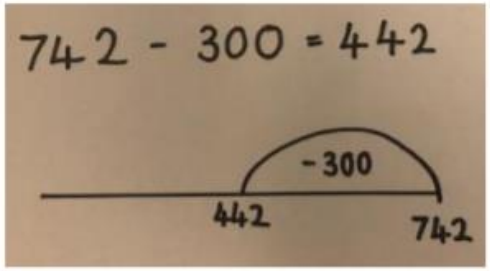
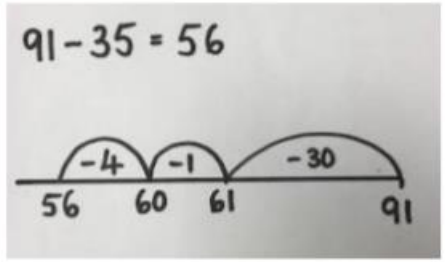
- subtract numbers mentally, including:
- a three-digit number and 1s
- a three-digit number and 10s
- a three-digit number and 100s
- subtract numbers with up to 3 digits, using formal written methods of columnar addition and subtraction
- solve problems, including missing number problems, using number facts, place value, and more complex subtraction

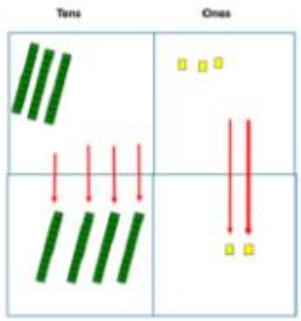
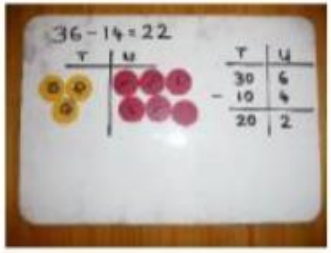
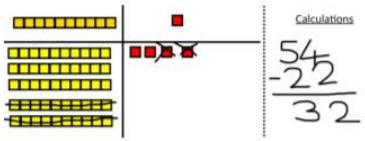
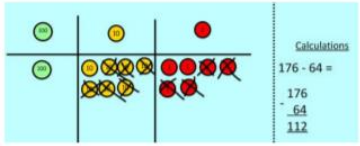
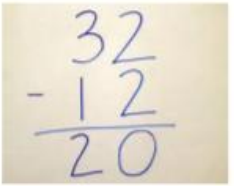
Children should also be taught to calculate the difference when two numbers are close in range e.g. 114 - 98, counting on 98 + 2 = 100 then 100 + 14 = 114, therefore the difference is 16 at all stages.

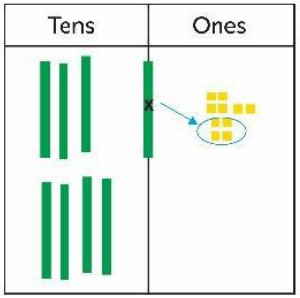
Bar models to be used to support decision making and where the missing numbers fit in our calculations.

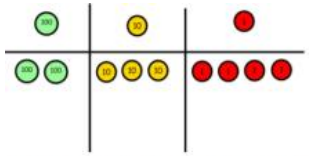
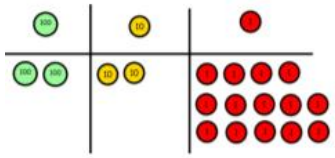
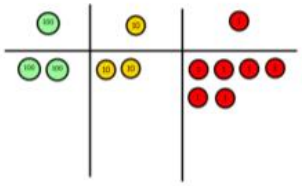
Make 10	14 - 9 = 	13 − 7 = 6 3 4 −4 −3 Start at 13. Take away 3 to reach 10. Then take away the remaining 4 so you have taken away 7 altogether. You have reached your answer.	16 - 8= How many do we take off to reach the next 10? How many do we have left to take off?

Subtract HTO – O (using bonds leading to partitioning)	135 – 2 = 133 		148 – 5 = 143 152-2=150 150-5=145 152 – 7 = 152 - 2 – 5 = 145
Subtract HTO – T (using bonds leading to partitioning)	135 – 20 = 115 		248 – 20 = 228 162 – 70 = 92 *162 – 60 = 102* *102 – 10 = 92*

Subtract HTO – H (using bonds)	635 – 400 = 235 		478 – 200 = 278
Subtract any TO – TO Using partitioning	**72 – 26 = 46** Use dienes and place value counters to model 72 – 20 – 2 – 4 = 46		**78 – 49 = 29** **78- 40= 38** **38-8=30** **30-1=39** 78 – 40 – 8 – 1 = 29

Column method without regrouping	 Use Base 10 to make the bigger number then take the smaller number away. Show how you partition numbers to subtract. Again make the larger number first. 	  Draw the Base 10 or place value counters alongside the written calculation to help to show working.	47 − 24 = 23 40 + 7 − 20 + 4 20 + 3 This will lead to a clear  written column subtraction.

Column method with regrouping	Use Base 10 to start with before moving on to place value counters. Start with one exchange before moving onto subtractions with 2 exchanges. Make the larger number with the place value counters 		 $\begin{array}{r} {}^{7}\cancel{8}\ {}^{1}0 \\ -\ 2\ \ 4 \\ \hline 6 \\ \hline \end{array}$

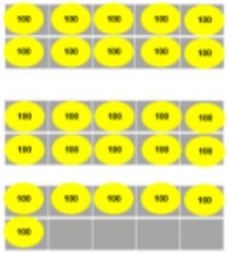
	 Calculations 234 - 88 Start with the ones, can I take away 8 from 4 easily? I need to exchange one of my tens for ten ones.  Calculations 234 - 88 Now I can subtract my ones.  Calculations 234 - 88 Now look at the tens, can I take away 8 tens easily? I need to exchange one hundred for ten tens.		

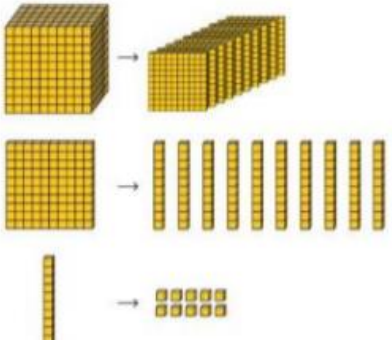
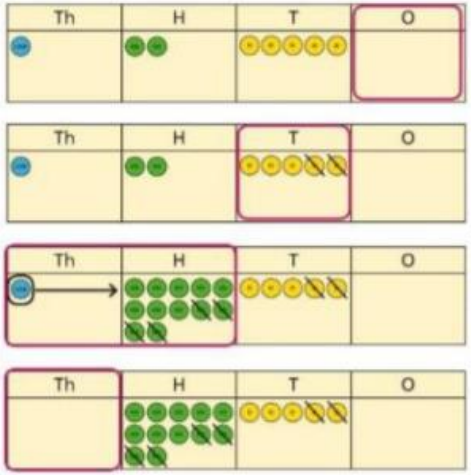
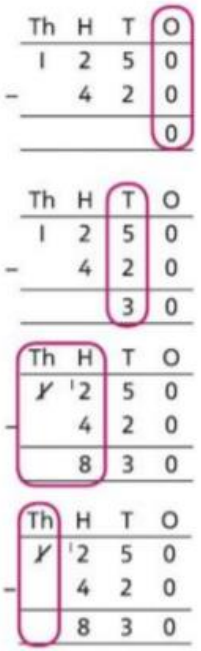
Subtraction Year 4

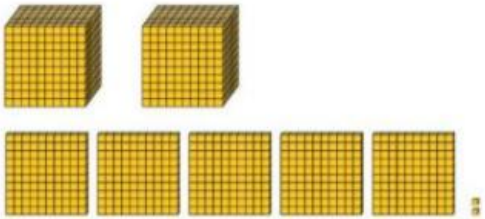
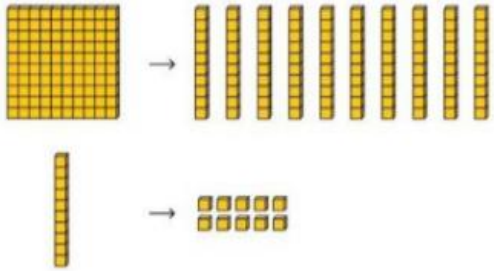
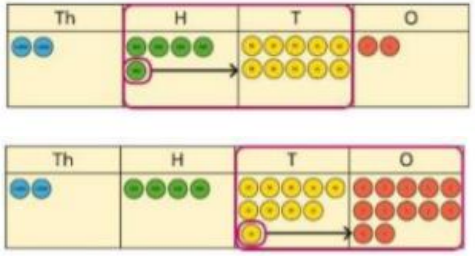
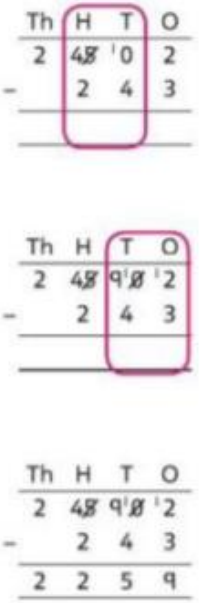
Pupils should be taught to:

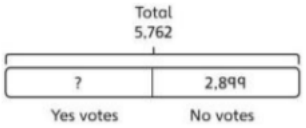
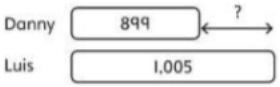
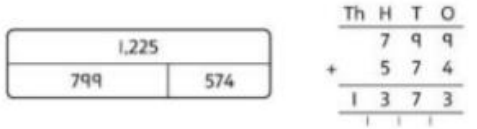
- subtract numbers with up to 4 digits using the formal written methods of columnar subtraction where appropriate
- estimate and use inverse operations to check answers to a calculation
- solve subtraction two-step problems in contexts, deciding which operations and methods to use and why

Bar models to be used to support decision making and where the missing numbers fit in our calculations.

Subtraction of multiples 10/100/1000	 2600 – 800		

Subtract with numbers up to four digits, including exchanging	Understand why exchange of a 1,000 for 100s, a 100 for 10s, or a 10 for 1s may be necessary. 	Represent place value equipment on a place value grid to subtract, including exchanges where needed. 	Use column subtraction, with understanding of the place value of any exchange required. 

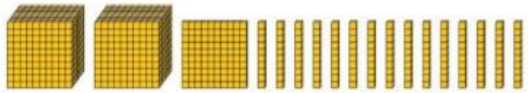
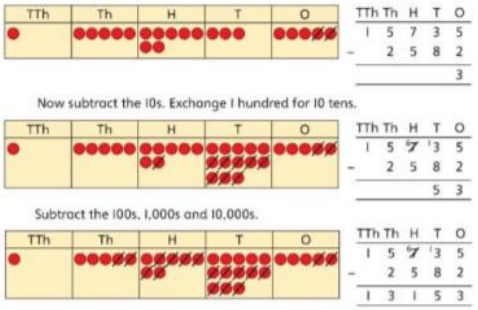
Column subtraction with exchange across more than one column	Understand why two exchanges may be necessary. *2,502 − 243 = ?*  *I need to exchange a 10 for some 1s, but there are not any 10s here.* 	Make exchanges across more than one column where there is a zero as a place holder. *2,502 − 243 = ?* 	Make exchanges across more than one column where there is a zero as a place holder. *2,502 − 243 = ?* 

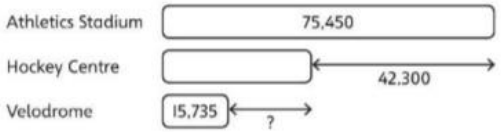
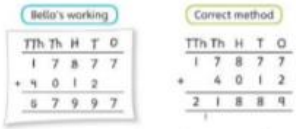
Representing subtractions and checking strategies		Use bar models to represent subtractions where a part needs to be calculated.  *I can work out the total number of Yes votes using 5,762 − 2,899.* Bar models can also represent 'find the difference' as a subtraction problem.  	Use inverse operations to check subtractions. *I calculated 1,225 − 799 = 574.* *I will check by adding the parts.*  *The parts do not add to make 1,225.* *I must have made a mistake.*

Subtraction Year 5

Pupils should be taught to:

- subtract whole numbers with more than 4 digits, including using formal written methods (columnar subtraction)
- subtract numbers mentally with increasingly large numbers
- solve subtraction multi-step problems in contexts, deciding which methods to use and why

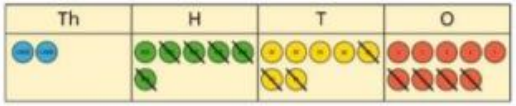
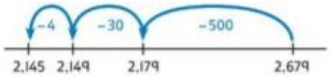
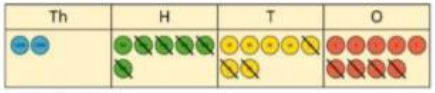
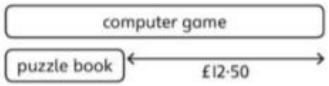
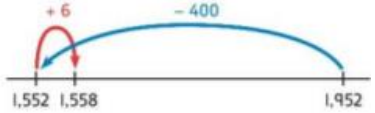
Column subtraction with whole numbers	Use place value equipment to understand where exchanges are required. *2,250 – 1,070* 	Represent the stages of the calculation using place value equipment on a grid alongside the calculation, including exchanges where required. *15,735 – 2,582 = 13,153*  	Use column subtraction methods with exchange where required. TTh Th H T O 5 11 1 0 9 7 – 1 8 5 3 4 4 3 5 6 3 *62,097 – 18,534 = 43,563*

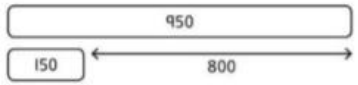
Checking strategies and representing subtractions		Bar models represent subtractions in problem contexts, including 'find the difference'.  	Children can explain the mistake made when the columns have not been ordered correctly.  Use approximation to check calculations. *I calculated 18,000 + 4,000 mentally to check my subtraction.*

Subtraction Year 6

Pupils should be taught to:

- perform mental calculations, including with increasingly large numbers
- use their knowledge of the order of operations to carry out calculation involving the 4 operations
- solve subtraction multi-step problems in contexts, deciding which methods to use and why
- solve problems using subtraction

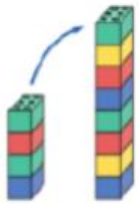
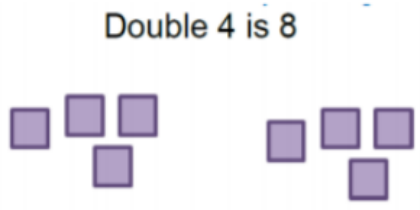
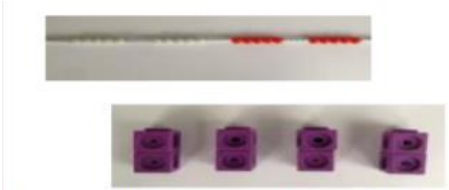
Comparing and selecting efficient methods	Use counters on a place value grid to represent subtractions of larger numbers.  	Compare subtraction methods alongside place value representations.   Th H T O 2 6 7 9 − 5 3 4 2 1 4 5 Use a bar model to represent calculations, including 'find the difference' with two bars as comparison.  	Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy. Th H T O 1 $^{8}\not{9}$ $^{14}\not{5}$ $^{1}2$ − 1 5 5 8 3 9 4  Use column subtraction for decimal problems, including in the context of measure. H T O · Tth Hth 3 0 9 · 6 0 − 2 0 6 · 4 0 1 0 3 · 2 0

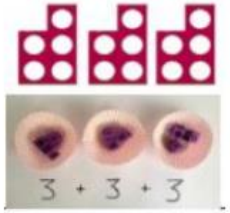
Subtracting mentally with larger numbers		Use a bar model to show how unitising can support mental calculations. *950,000 − 150,000* *That is 950 thousands − 150 thousands*  *So, the difference is 800 thousands.* *950,000 − 150,000 = 800,000*	Subtract efficiently from powers of 10. *10,000 − 500 = ?*

Year 1 Multiplication

Pupils should be taught to:

- solve one-step problems involving multiplication by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher

Doubling	Use practical activities to show how to double a number.  double 4 is 8 4 × 2 = 8	Draw pictures to show how to double a number. 	Show calculation 3 groups of 2 = 6
Counting in multiples	 Count in multiples supported by concrete objects in equal groups.		Count in multiples of a number aloud. Write sequences with multiples of numbers. 2, 4, 6, 8, 10 5, 10, 15, 20, 25 , 30

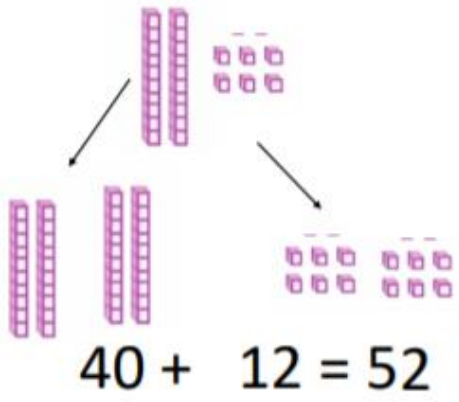
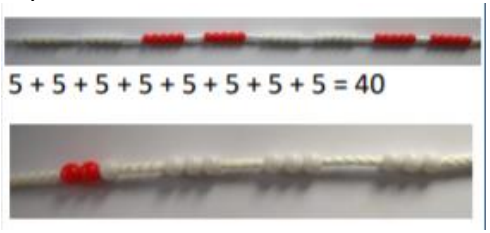
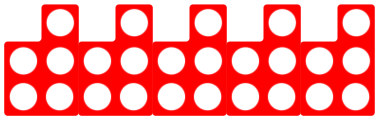
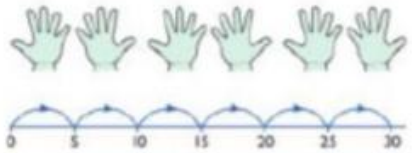
Repeated addition	Use different objects to add equal groups.  		Write addition sentences to describe objects and pictures. 

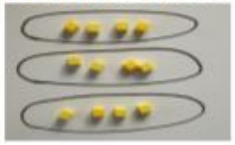
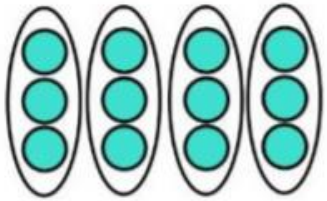
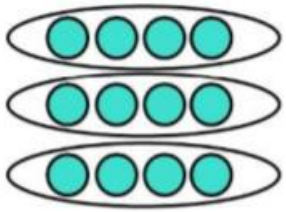
Year 2 Multiplication

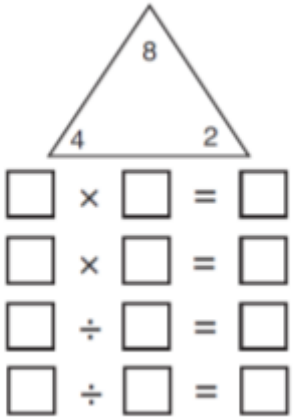
Pupils should be able to:

- recall and use multiplication facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers calculate mathematical statements for multiplication a within the multiplication tables and write them using the multiplication (×) and equals (=) signs
- show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot
- solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

Objective and strategy	Concrete	Pictorial	Abstract
Doubling	Model doubling using base ten by partitioning tens and ones. Then double the tens and double the ones. Make the total amount. Double 26 : 26 x 2 =	Draw pictures and representations to show how to double numbers.	26 x 2

			
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Using different manipulatives to make repeated additions sums.  5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40 3 + 3 + 3 + 3 = 12 3x4=12  5 + 5 + 5 + 5 + 5 = 25 5x5=25	Number lines, counting sticks and bar models should be used to show repre-sentation of counting in multiples. 	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25 , 30 $4 \times 3 = \square$

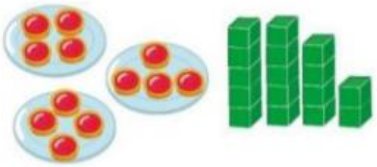
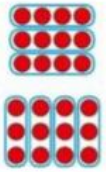
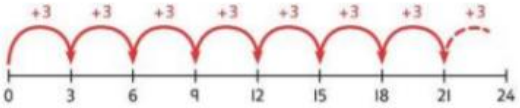
Multiplication is commutative.	Create arrays using counters, numicon and cubes.   Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.  	Use representations of arrays to show different calculations and explore commutativity.  	12 = 3 × 4 12 = 4 × 3 Use an array to write multiplication sentences and reinforce repeated addition.  5 + 5 + 5 = 15 3 + 3 + 3 + 3 + 3 = 15 5 x 3 = 15 3 x 5 = 15

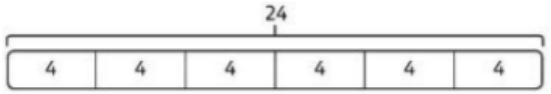
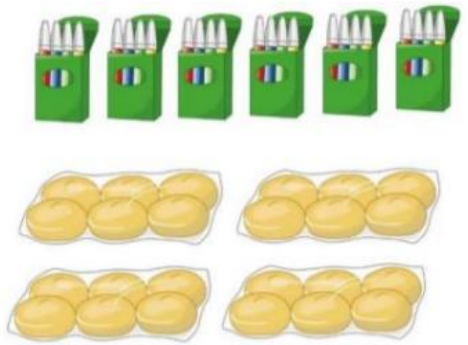
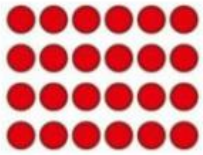
Using the Inverse This should be taught alongside division, so pupils learn how they work alongside each other.			2 x 4 = 8 4 x 2 = 8 8 ÷ 2 = 4 8 ÷ 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 ÷ 4 4 = 8÷ 2 Show all 8 related fact family sentences.

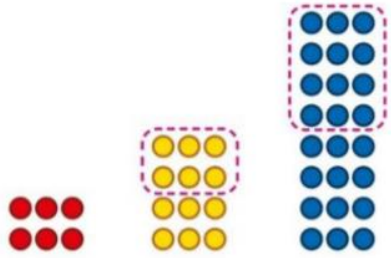
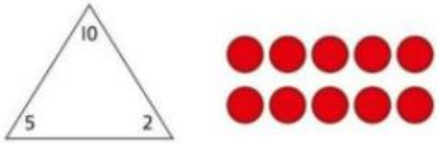
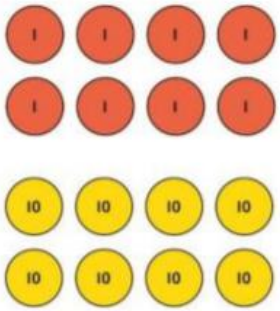
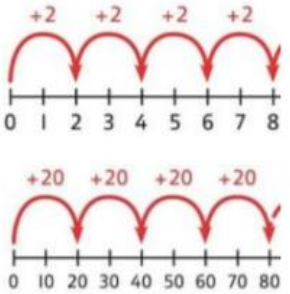
Year 3 Multiplication

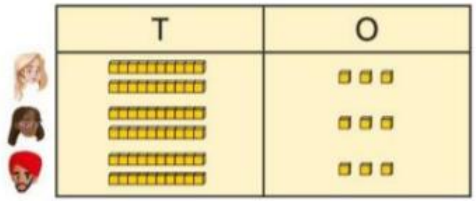
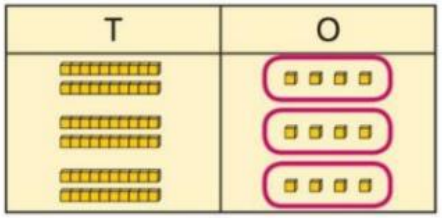
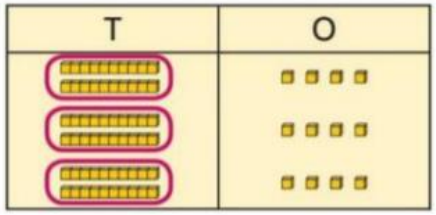
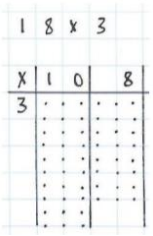
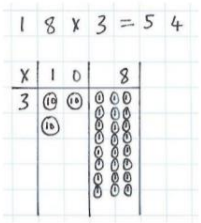
Pupils should be taught to:

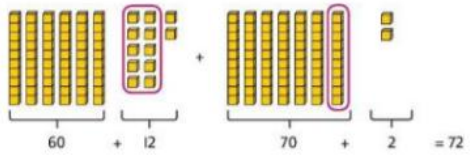
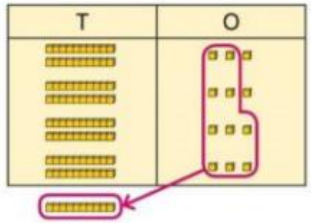
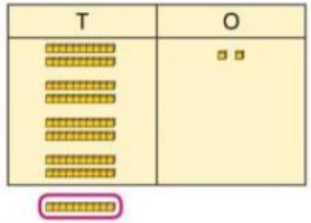
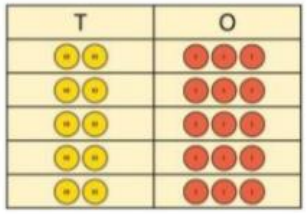
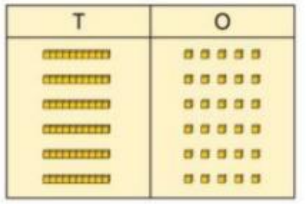
- recall and use multiplication facts for the 3,4 and 8 multiplication tables
- write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
- solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in with n objects are connected to m objects

Understanding equal grouping and repeated addition	Children continue to build understanding of equal groups and the relationship with repeated addition. They recognise both examples and non-examples using objects. 	Children recognise that arrays demonstrate commutativity.  *This is 3 groups of 4.* *This is 4 groups of 3.*	Children understand the link between repeated addition and multiplication.  *8 groups of 3 is 24.* *3 + 3 + 3 + 3 + 3 + 3 + 3 + 3 = 24* *8 × 3 = 24*

	Children recognise that arrays can be used to model commutative multiplications.  *I can see 3 groups of 8.* *I can see 8 groups of 3.*		A bar model may represent multiplications as equal groups.  *6 × 4 = 24*
Using commutativity to support understanding of the times tables	Understand how to use times-tables facts flexibly.  *There are 6 groups of 4 pens.* *There are 4 groups of 6 bread rolls.* *I can use 6 × 4 = 24 to work out both totals.*	Understand how times-table facts relate to commutativity.  *6 × 4 = 24* *4 × 6 = 24*	Understand how times-table facts relate to commutativity. *I need to work out 4 groups of 7.* *I know that 7 × 4 = 28* *so, I know that* *4 groups of 7 = 28* *and* *7 groups of 4 = 28.*

Understanding and using ×3, ×2, ×4 and ×8 tables.	Children learn the times-tables as 'groups of', but apply their knowledge of commutativity.  *I can use the ×3 table to work out how many keys.* *I can also use the ×3 table to work out how many batteries.*	Children understand how the ×2, ×4 and ×8 tables are related through repeated doubling.  3 × 2 = 6 3 × 4 = 12 3 × 8 = 24	Children understand the relationship between related multiplication and division facts in known times-tables.  *2 × 5 = 10* *5 × 2 = 10* *10 ÷ 5 = 2* *10 ÷ 2 = 5*
Using known facts to multiply 10s, for example 3 × 40	Explore the relationship between known times-tables and multiples of 10 using place value equipment. *Make 4 groups of 3 ones.*  *Make 4 groups of 3 tens.*  *What is the same?* *What is different?*	Understand how unitising 10s supports multiplying by multiples of 10.  *4 groups of 2 ones is 8 ones.* *4 groups of 2 tens is 8 tens.* *4 × 2 = 8* *4 × 20 = 80*	Understand how to use known times-tables to multiply multiples of 10.  *4 × 2 = 8* *4 × 20 = 80*

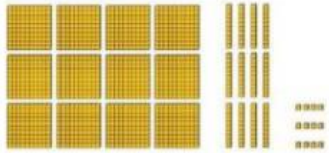
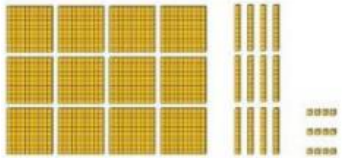
Multiplying a 2-digit number by a 1-digit number	Understand how to link partitioning a 2-digit number with multiplying. *Each person has 23 flowers.* *Each person has 2 tens and 3 ones.*  *There are 3 groups of 2 tens.* *There are 3 groups of 3 ones.* Use place value equipment to model the multiplication context.  *There are 3 groups of 3 ones.* *There are 3 groups of 2 tens.*	Use place value to support how partitioning is linked with multiplying by a 2-digit number. *3 × 24 = ?*  *3 × 4 = 12*  *3 × 20 = 60* *60 + 12 = 72* *3 × 24 = 72*	Use addition to complete multiplications of 2-digit numbers by a 1-digit number. *4 × 13 = ?* *4 × 3 = 12* *4 × 10 = 40* *12 + 40 = 52* *4 × 13 = 52*  The two digit number is partitioned horizontally with the tens digit coming first. The equation is then represented using counters (or an array).  Again, the two digit number is partitioned horizontally with the tens digit coming first. This time the equation is represented using place value counters or Dienes.

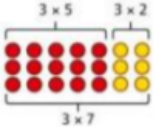
Multiplying a 2-digit number by a 1-digit number, expanded column method	Use place value equipment to model how 10 ones are exchanged for a 10 in some multiplications. *3 × 24 = ?* *3 × 20 = 60* *3 × 4 = 12*  *3 × 24 = 60 + 12* *3 × 24 = 70 + 2* *3 × 24 = 72*	Understand that multiplications may require an exchange of 1s for 10s, and also 10s for 100s. *4 × 23 = ?*   *4 × 23 = 92*  *5 × 23 = ?* *5 × 3 = 15* *5 × 20 = 100* *5 × 23 = 115*	Children may write calculations in expanded column form, but must understand the link with place value and exchange. Children are encouraged to write the expanded parts of the calculation separately.  T O 1 5 × 6 + 6 × 5 6 × 10 *5 × 28 = ?* T O 2 8 × 5 4 0 5 × 8 1 0 0 5 × 20 1 4 0

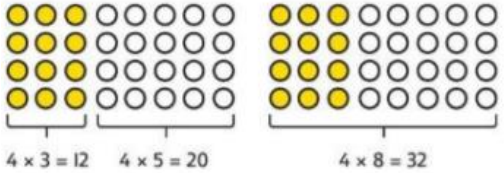
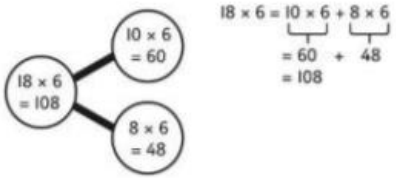
Year 4 Multiplication

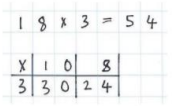
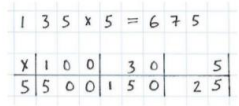
Pupils should be taught to:

- recall multiplication facts for multiplication tables up to 12 x 12
- use place value, known and derived facts to multiply mentally, including: multiplying by 0 and 1; multiplying together 3 numbers
- recognise and use factor pairs and commutativity in mental calculations
- multiply two-digit and three-digit numbers by a one-digit number using formal written layout
- solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by 1 digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects

Multiplying by multiples of 10 and 100	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.  *3 groups of 4 ones is 12 ones.* *3 groups of 4 tens is 12 tens.* *3 groups of 4 hundreds is 12 hundreds.*	Use unitising and place value equipment to understand how to multiply by multiples of 1, 10 and 100.  *3 × 4 = 12* *3 × 40 = 120* *3 × 400 = 1,200*	Use known facts and understanding of place value and commutativity to multiply mentally. *4 × 7 = 28* *4 × 70 = 280* *40 × 7 = 280* *4 × 700 = 2,800* *400 × 7 = 2,800*

Understanding times-tables up to 12 × 12	Understand the special cases of multiplying by 1 and 0.  *5 × 1 = 5* *5 × 0 = 0*	Represent the relationship between the ×9 table and the ×10 table.  Represent the ×11 table and ×12 tables in relation to the ×10 table.  *2 × 11 = 20 + 2* *3 × 11 = 30 + 3* *4 × 11 = 40 + 4*  *4 × 12 = 40 + 8*	Understand how times-tables relate to counting patterns. Understand links between the ×3 table, ×6 table and ×9 table *5 × 6 is double 5 × 3* ×5 table and ×6 table *I know that 7 × 5 = 35* *so I know that 7 × 6 = 35 + 7.* ×5 table and ×7 table *3 × 7 = 3 × 5 + 3 × 2*  ×9 table and ×10 table *6 × 10 = 60* *6 × 9 = 60 − 6* **Speaking Frame - Counting in Multiples** We are using _____ to count in multiples of ☐ The ☐ multiple of ☐ is ☐ This could also be ☐ + ☐ + ☐ + ☐ ... ☐ groups of ☐ is ☐ This is also ☐ x ☐ =

Understanding and using partitioning in multiplication	Make multiplications by partitioning. *4 × 12 is 4 groups of 10 and 4 groups of 2.*  *4 × 12 = 40 + 8*	Understand how multiplication and partitioning are related through addition.  *4 × 3 = 12* *4 × 5 = 20* *12 + 20 = 32* *4 × 8 = 32*	Use partitioning to multiply 2-digit numbers by a single digit. *18 × 6 = ?*  *18 × 6 = 10 × 6 + 8 × 6* *= 60 + 48* *= 108*
Column multiplication for 2- and 3-digit numbers multiplied by a single digit	Use place value equipment to make multiplications. *Make 4 × 136 using equipment.*  *I can work out how many 1s, 10s and 100s.* *There are 4 × 6 ones… 24 ones* *There are 4 × 3 tens … 12 tens* *There are 4 × 1 hundreds … 4 hundreds* *24 + 120 + 400 = 544*	Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit.  3 1 2 × 3 9 3 6	Use the formal column method for up to 3-digit numbers multiplied by a single digit. 3 1 2 × 3 9 3 6 Understand how the expanded column method is related to the formal column method and understand how any exchanges are related to place value at each stage of the calculation. 2 3 × 5 1 5 1 0 0 1 1 5 2 3 × 5 1 1 5 1

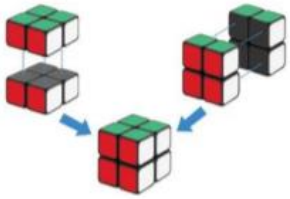
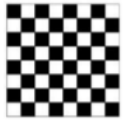
			3. Grid method (using place value counters or Dienes) • TO x O  The same layout is used as before but this time, the digits are being used. • HTO x O  The three digit number is partitioned horizontally with the hundreds first followed by the tens and ones.

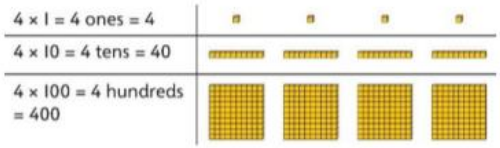
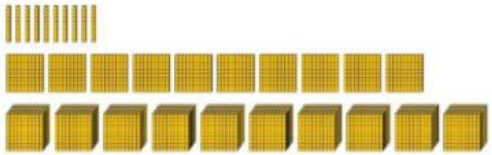
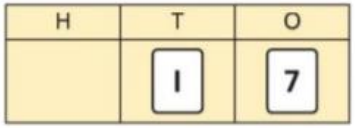
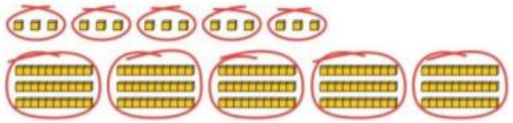
Multiplying more than two numbers	Represent situations by multiplying three numbers together.  *Each sheet has 2 × 5 stickers.* *There are 3 sheets.* *There are 5 × 2 × 3 stickers in total.* 5 × 2 × 3 = 30 10 × 3 = 30	Understand that commutativity can be used to multiply in different orders.  *2 × 6 × 10 = 120* *12 × 10 = 120* *10 × 6 × 2 = 120* *60 × 2 = 120*	Use knowledge of factors to simplify some multiplications. *24 × 5 = 12 × 2 × 5* 12 × 2 × 5 = 12 × 10 = 120 So, 24 × 5 = 120

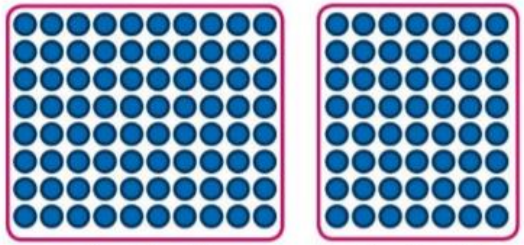
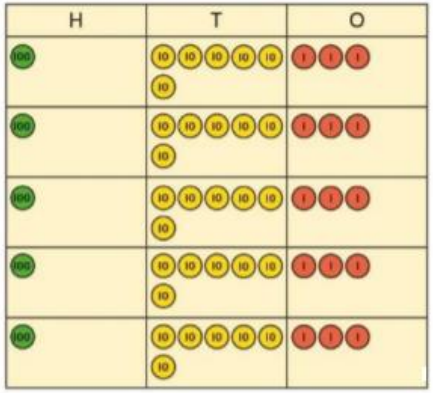
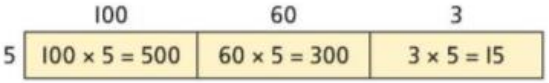
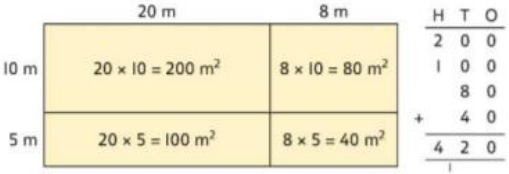
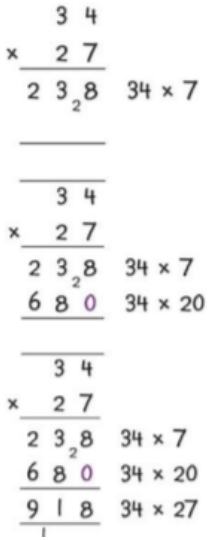
Year 5 Multiplication

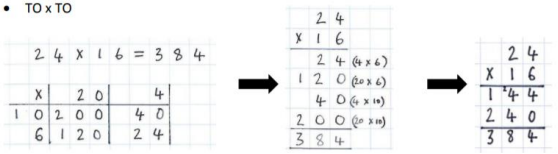
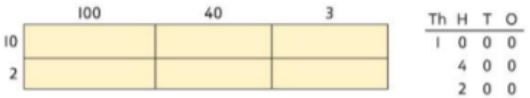
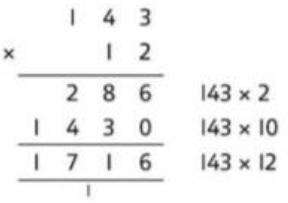
Pupils should be taught to:

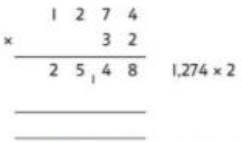
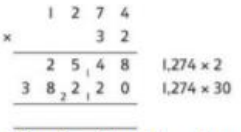
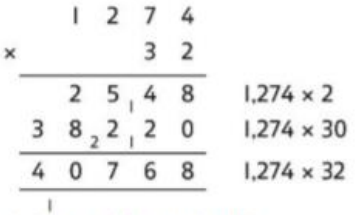
- multiply numbers up to 4 digits by a one- or two digit number using a formal written method, including long multiplication for two-digit numbers
- multiply numbers mentally, drawing upon known facts
- multiply whole numbers and those involving decimals by 10,100 and 1,000
- solve problems involving multiplication, including using their knowledge of factors and multiples, squares and cubes
- solve problems involving multiplication including understanding the meaning of the equals sign

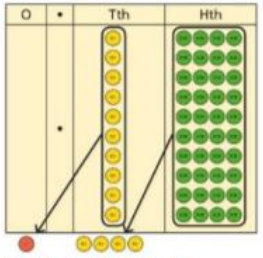
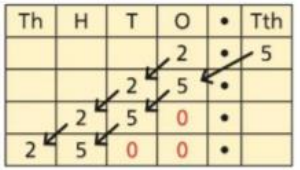
Understanding factors	Use cubes or counters to explore the meaning of 'square numbers'. *25 is a square number because it is made from 5 rows of 5.* Use cubes to explore cube numbers.  *8 is a cube number.*	Use images to explore examples and non-examples of square numbers.  *8 × 8 = 64* *8^2 = 64*  *12 is not a square number, because you cannot multiply a whole number by itself to make 12.*	Understand the pattern of square numbers in the multiplication tables. Use a multiplication grid to circle each square number. Can children spot a pattern?

Multiplying by 10, 100 and 1,000	Use place value equipment to multiply by 10, 100 and 1,000 by unitising.  	Understand the effect of repeated multiplication by 10. 	Understand how exchange relates to the digits when multiplying by 10, 100 and 1,000.  *17 × 10 = 170* *17 × 100 = 17 × 10 × 10 = 1,700* *17 × 1,000 = 17 × 10 × 10 × 10 = 17,000*
Multiplying by multiples of 10, 100 and 1,000	Use place value equipment to explore multiplying by unitising.  *5 groups of 3 ones is 15 ones.* *5 groups of 3 tens is 15 tens.* *So, I know that 5 groups of 3 thousands would be 15 thousands.*	Use place value equipment to represent how to multiply by multiples of 10, 100 and 1,000.  *4 × 3 = 12* *4 × 300 = 1,200* *6 × 4 = 24* *6 × 400 = 2,400*	Use known facts and unitising to multiply. *5 × 4 = 20* *5 × 40 = 200* *5 × 400 = 2,000* *5 × 4,000 − 20,000* *5,000 × 4 = 20,000*

Multiplying up to 4-digit numbers by a single digit	Explore how to use partitioning to multiply efficiently. *8 × 17 = ?*  8 × 10 = 80 8 × 7 = 56 80 + 56 = 136 *So, 8 × 17 = 136*	Represent multiplications using place value equipment and add the 1s, then 10s, then 100s, then 1,000s.  	Use an area model and then add the parts.  Use a column multiplication, including any required exchanges. 
Multiplying 2-digit numbers by 2-digit numbers	Partition one number into 10s and 1s, then add the parts. *23 × 15 = ?*  10 × 15 = 150 10 × 15 = 150  3 × 15 = 45 There are 345 bottles of milk in total.  *23 × 15 = 345*	Use an area model and add the parts. *28 × 15 = ?*  *28 × 15 = 420*	Use column multiplication, ensuring understanding of place value at each stage. 

			5. Long Multiplication (introduced alongside grid method) • TO x TO 
Multiplying up to 4-digits by 2-digits		Use the area model then add the parts.   143 × 12 = 1,716 There are 1,716 boxes of cereal in total. ***143 × 12 = 1,716***	Use column multiplication, ensuring understanding of place value at each stage.  Progress to include examples that require multiple exchanges as understanding, confidence and fluency build.

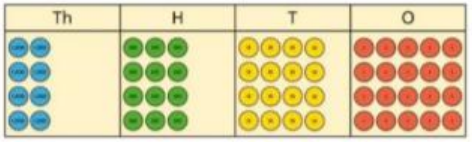
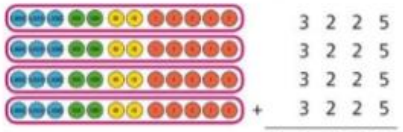
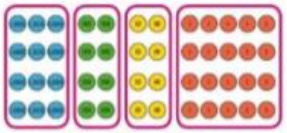
			1,274 × 32 = ? *First multiply 1,274 by 2.*  *Then multiply 1,274 by 30.*  *Finally, find the total.*  *1,274 × 32 = 40,768*

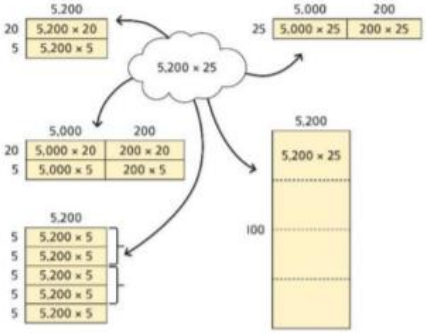
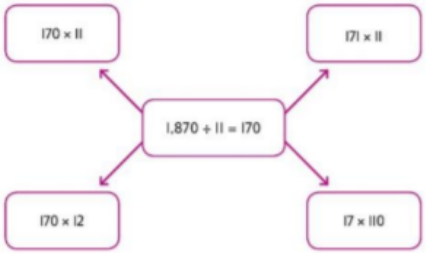
Multiplying decimals by 10, 100 and 1,000	Use place value equipment to explore and understand the exchange of 10 tenths, 10 hundredths or 10 thousandths.	Represent multiplication by 10 as exchange on a place value grid.  *0·14 × 10 = 1·4*	Understand how this exchange is represented on a place value chart. 2·5 × 10 = 25 2·5 × 100 = 250 2·5 × 1,000 = 2,500 

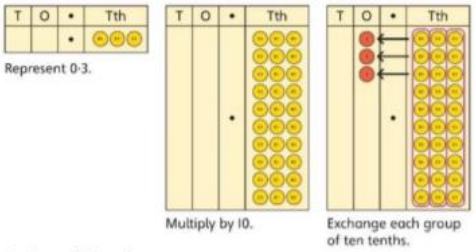
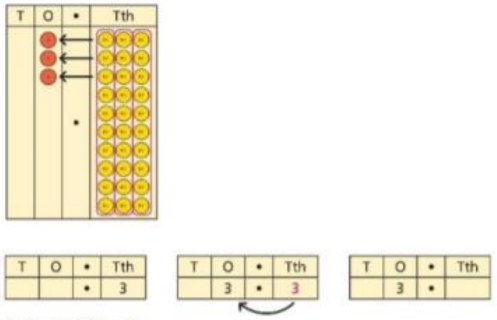
Year 6 Multiplication

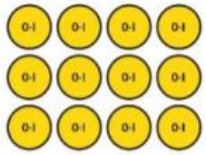
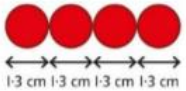
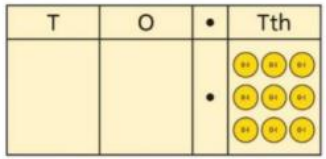
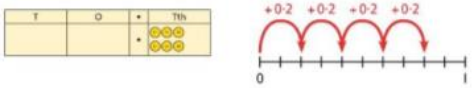
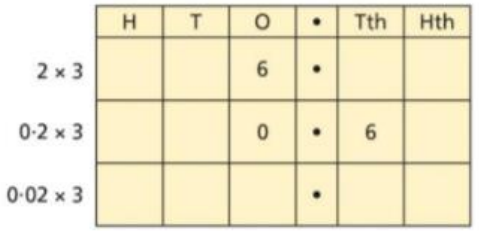
Pupils should be taught to:

- multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication
- perform mental calculations, including with mixed operations and large numbers
- use their knowledge of the order of operation to carry out calculations involving the 4 operations
- solve problems involving multiplication

Multiplying up to a 4-digit number by a single digit number	Use equipment to explore multiplications.  *4 groups of 2,345* *This is a multiplication:* *4 × 2,345* *2,345 × 4*	Use place value equipment to compare methods. Method 1  3 2 2 5 3 2 2 5 3 2 2 5 + 3 2 2 5 1 2 9 0 0 Method 2  4 × 3,000 4 × 200 4 × 20 4 × 5 12,000 + 800 + 80 + 20 = 12,900	Understand area model and short multiplication. Compare and select appropriate methods for specific multiplications. Method 3 3,000 200 20 5 4 | 12,000 | 800 | 80 | 20 12,000 + 800 + 80 + 20 = 12,900 Method 4 3 2 2 5 × 4 1 2 9 0 0

Multiplying up to a 4-digit number by a 2-digit number		Use an area model alongside written multiplication. **Method I** 1,235 × 21 1,000 200 30 5 20 20,000 4,000 600 100 1 1,000 200 30 5 1 2 3 5 × 2 1 5 (1 × 5) 3 0 (1 × 30) 2 0 0 (1 × 200) 1 0 0 0 (1 × 1,000) 1 0 0 (20 × 5) 6 0 0 (20 × 30) 4 0 0 0 (20 × 200) 2 0 0 0 0 (20 × 1,000) 2 5 9 3 5 (21 × 1,235)	Use compact column multiplication with understanding of place value at all stages. 1 2 3 5 × 2 1 1 2 3 5 (1 × 1,235) 2 4 7 0 0 (20 × 1,235) 2 5 9 3 5 (21 × 1,235) • HTO x TO 262 x 19 = 4,978 x 200 60 2 10 2,000 600 20 2620 9 1800 540 18 2358 4,978 262 x 19 2358 2620 4,978
Using knowledge of factors and partitions to compare methods for multiplications	Use equipment to understand square numbers and cube numbers.  $5 \times 5 = 5^2 = 25$ $5 \times 5 \times 5 = 5^3 = 25 \times 5 = 125$	Compare methods visually using an area model. Understand that multiple approaches will produce the same answer if completed accurately.  Represent and compare methods using a bar model.	Use a known fact to generate families of related facts.  Use factors to calculate efficiently. 15×16 $= 3 \times 5 \times 2 \times 8$ $= 3 \times 8 \times 2 \times 5$ $= 24 \times 10$ $= 240$

Multiplying by 10, 100 and 1,000	Use place value equipment to explore exchange in decimal multiplication.  *0·3 × 10 = ?* *0·3 is 3 tenths.* *10 × 3 tenths are 30 tenths.* *30 tenths are equivalent to 3 ones.*	Understand how the exchange affects decimal numbers on a place value grid.  *0·3 × 10 = 3*	Use knowledge of multiplying by 10, 100 and 1,000 to multiply by multiples of 10, 100 and 1,000. *8 × 100 = 800* *8 × 300 = 800 × 3* *= 2,400* *2·5 × 10 = 25* *2·5 × 20 = 2·5 × 10 × 2* *= 50* **Oracy** **I know 1 x 3 = 3. So I also know** **1 x 0.3 = 0.3** **10 x 0.3 = 3.0** **1 x 0.03 = 0.03** **10 x 0.03 = 0.3**

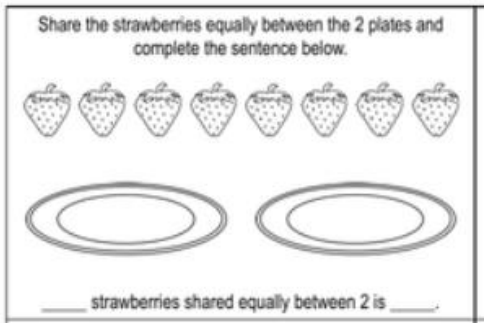
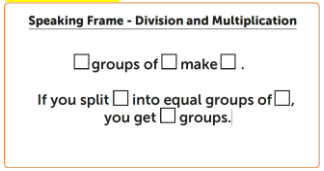
Multiplying decimals	Explore decimal multiplications using place value equipment and in the context of measures.  *3 groups of 4 tenths is 12 tenths.* *4 groups of 3 tenths is 12 tenths.*  *4 × 1 cm = 4 cm* *4 × 0·3 cm = 1.2 cm* *4 × 1·3 = 4 + 1·2 = 5·2 cm*	Represent calculations on a place value grid. 3 × 3 = 9 3 × 0·3 = 0·9  Understand the link between multiplying decimals and repeated addition. 	Use known facts to multiply decimals. *4 × 3 = 12* *4 × 0·3 = 1·2* *4 × 0·03 = 0·12* *20 × 5 = 100* *20 × 0·5 = 10* *20 × 0·05 = 1* Find families of facts from a known multiplication. *I know that 18 × 4 = 72.* *This can help me work out:* *1·8 × 4 = ?* *18 × 0·4 = ?* *180 × 0·4 = ?* *18 × 0·04 = ?* Use a place value grid to understand the effects of multiplying decimals. 

	H	T	O	•	Tth	Hth
2 × 3			6	•		
0·2 × 3			0	•	6	
0·02 × 3				•		

Year 1 Division

Pupils should be taught to:

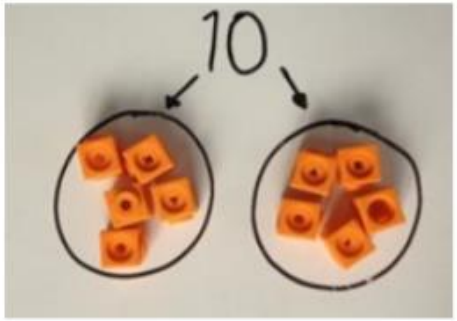
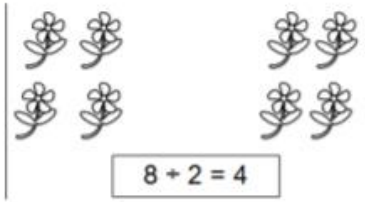
- solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher

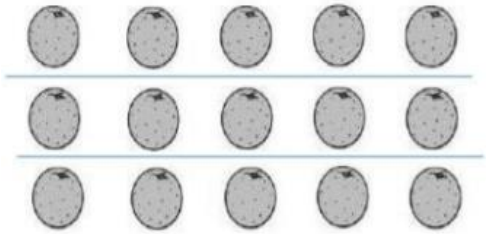
Division as sharing	Practice sharing into equal groups. 		Complete a division calculation If you split ___into equal groups of___ , you get___ groups. 

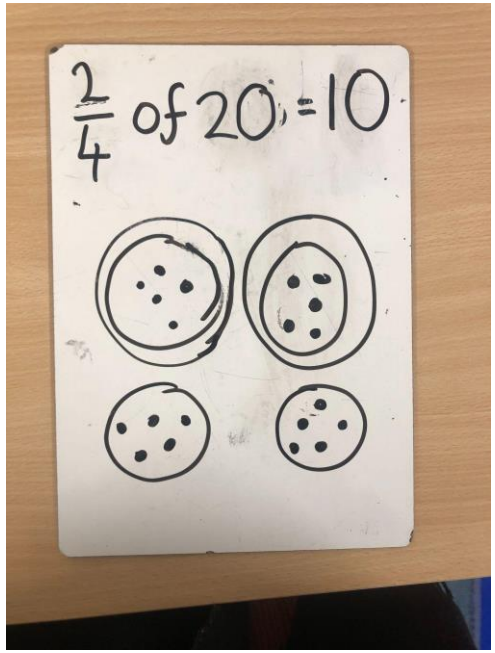
Year 2 Division

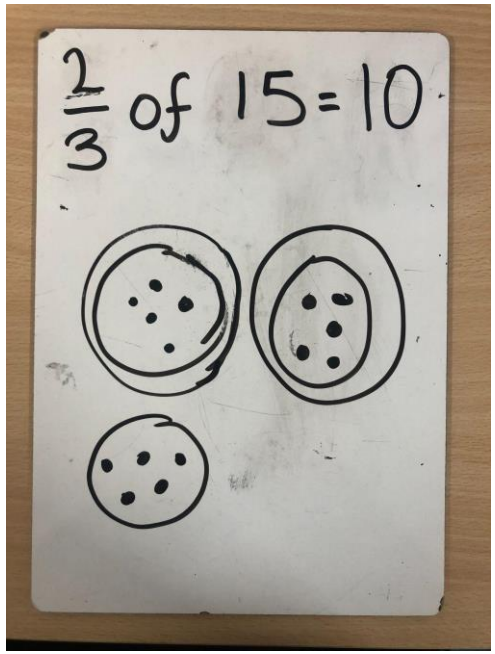
Pupils should be able to:

- recall and use division facts for the 2, 5 and 10
- calculate mathematical statements for multiplication and division
- write the division (÷) and equals (=) signs
- show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

Objectives and strategies	Concrete	Pictorial	Abstract
Division as sharing	 I have 10 cubes, can you share them equally in 2 groups?	Children use pictures or shapes to share quantities.  Draw sharing model to support division and halving. Half of 10 is -	28 ÷ 7 = 4 Divide 28 into 7 groups. How many are in each group?

Division as grouping	Division by grouping- Group objects into their divisible factor.	Draw an array and use lines to split the array into groups to make multiplication and division sentences. 	Find the inverse of multiplication and division sentences by creating four linking number sentences. **7 x 4 = 28** **4 x 7 = 28** **28 ÷ 7 = 4** **28 ÷ 4 = 7**
Division within arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created.  Eg. **15 ÷ 3 = 5** **5 x 3 = 15** **15 ÷ 5 = 3** **3 x 5 = 15**		

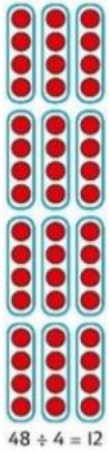
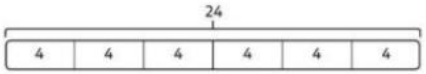
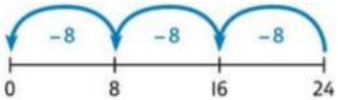
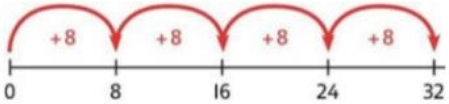
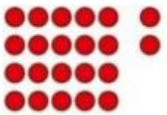
Division in quarters	Dividing objects into 4 groups and counting the fraction of the amount.		2/4 of 20 = 10

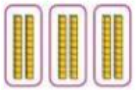
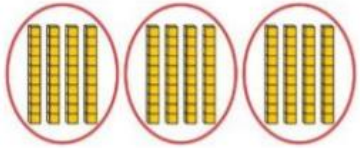
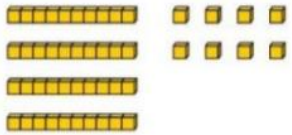
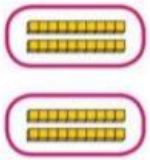
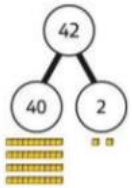
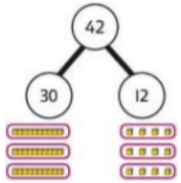
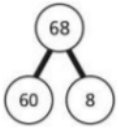
Division in thirds	Dividing objects into 3 groups and counting the fraction of the amount.		⅔ of 15 = 10

Year 3 Division

Pupils should be taught to:

- recall and use division facts for the 3, 4 and 8 multiplication tables
- write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
- solve problems, including missing number problems, involving division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects

Using times tables knowledge to divide	Use knowledge of known times-tables to calculate divisions.  *24 divided into groups of 8.* *There are 3 groups of 8.*	Use knowledge of known times-tables to calculate divisions.  48 ÷ 4 = 12 *48 divided into groups of 4.* *There are 12 groups.* *4 × 12 = 48* *48 ÷ 4 = 12*	Use knowledge of known times-tables to calculate divisions. *I need to work out 30 shared between 5.* *I know that 6 × 5 = 30* *so I know that 30 ÷ 5 = 6.* A bar model may represent the relationship between sharing and grouping.  *24 ÷ 4 = 6* *24 ÷ 6 = 4* Children understand how division is related to both repeated subtraction and repeated addition.  *24 ÷ 8 = 3*  *32 ÷ 8 = 4*
Understanding remainders	Use equipment to understand that a remainder occurs when a set of objects cannot be divided equally any further.  *There are 13 sticks in total.* *There are 3 groups of 4, with 1 remainder.*	Use images to explain remainders.  *22 ÷ 5 = 4 remainder 2*	Understand that the remainder is what cannot be shared equally from a set. *22 ÷ 5 = ?* *3 × 5 = 15* *4 × 5 = 20* *5 × 5 = 25 … this is larger than 22* *So, 22 ÷ 5 = 4 remainder 2*

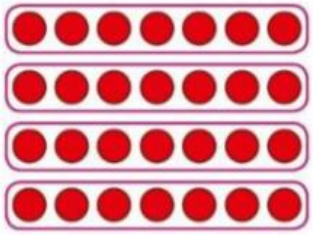
Using known facts to divide multiples of 10	Use place value equipment to understand how to divide by unitising. *Make 6 ones divided by 3.*  *Now make 6 tens divided by 3.*  *What is the same? What is different?*	Divide multiples of 10 by unitising.  *12 tens shared into 3 equal groups.* *4 tens in each group.*	Divide multiples of 10 by a single digit using known times-tables. *180 ÷ 3 = ?* *180 is 18 tens.* *18 divided by 3 is 6.* *18 tens divided by 3 is 6 tens.* *18 ÷ 3 = 6* *180 ÷ 3 = 60*
2-digit number divided by 1-digit number, no remainders	Children explore dividing 2-digit numbers by using place value equipment.  *48 ÷ 2 = ?* *First divide the 10s.*  *Then divide the 1s.* 	Children explore which partitions support particular divisions.  *I need to partition 42 differently to divide by 3.*  *42 = 30 + 12* *42 ÷ 3 = 14*	Children partition a number into 10s and 1s to divide where appropriate.  *60 ÷ 2 = 30* *8 ÷ 2 = 4* *30 + 4 = 34* *68 ÷ 2 = 34*

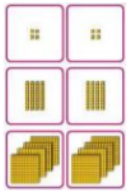
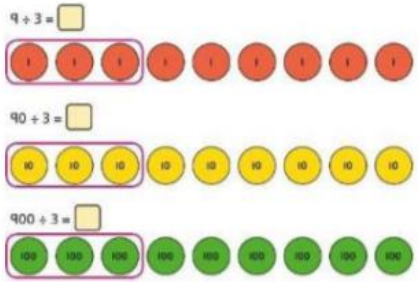
			Children partition flexibly to divide where appropriate. *42 ÷ 3 = ?* *42 = 40 + 2* *I need to partition 42 differently to divide by 3.* *42 = 30 + 12* *30 ÷ 3 = 10* *12 ÷ 3 = 4* *10 + 4 = 14* *42 ÷ 3 = 14*
2-digit number divided by 1-digit number, with remainders	Use place value equipment to understand the concept of remainder. *Make 29 from place value equipment. Share it into 2 equal groups.*  *There are two groups of 14 and 1 remainder.*	Use place value equipment to understand the concept of remainder in division. *29 ÷ 2 = ?*  *29 ÷ 2 = 14 remainder 1*	Partition to divide, understanding the remainder in context. *67 children try to make 5 equal lines.* *67 = 50 + 17* *50 ÷ 5 = 10* *17 ÷ 5 = 3 remainder 2* *67 ÷ 5 = 13 remainder 2* *There are 13 children in each line and 2 children left out.*

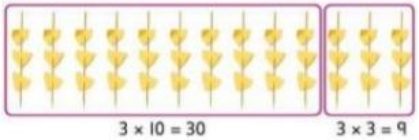
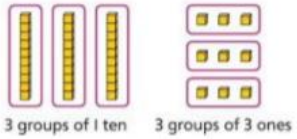
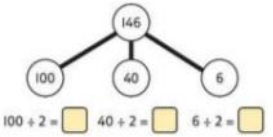
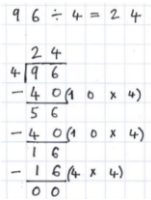
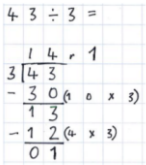
Year 4 Division

Pupils should be taught to:

- recall division facts for multiplication tables up to 12 x 12
- use place value, known and derived facts to divide mentally
- recognise and use factor pairs and commutativity in mental calculations
- multiply two-digit and three-digit numbers by a one-digit number using formal written layout
- solve problems involving multiplying and adding, including using the distributive law to multiply two-digit numbers by 1 digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects

Understanding the relationship between multiplication and division, including times-tables	Use objects to explore families of multiplication and division facts.  *4 × 6 = 24* *24 is 6 groups of 4.* *24 is 4 groups of 6.* *24 divided by 6 is 4.* *24 divided by 4 is 6.*	Represent divisions using an array.  28 ÷ 7 = 4	Understand families of related multiplication and division facts. *I know that 5 × 7 = 35* *so I know all these facts:* *5 × 7 = 35* *7 × 5 = 35* *35 = 5 × 7* *35 = 7 × 5* *35 ÷ 5 = 7* *35 ÷ 7 = 5* *7 = 35 ÷ 5* *5 = 35 ÷ 7*

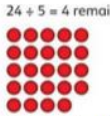
Dividing multiples of 10 and 100 by a single digit	Use place value equipment to understand how to use unitising to divide.  *8 ones divided into 2 equal groups* *4 ones in each group* *8 tens divided into 2 equal groups* *4 tens in each group* *8 hundreds divided into 2 equal groups* *4 hundreds in each group*	Represent divisions using place value equipment.  *9 ÷ 3 = 3* *9 tens divided by 3 is 3 tens.* *9 hundreds divided by 3 is 3 hundreds.*	Use known facts to divide 10s and 100s by a single digit. *15 ÷ 3 = 5* *150 ÷ 3 = 50* *1500 ÷ 3 = 500*

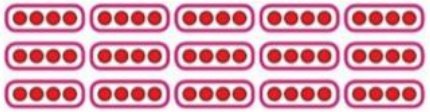
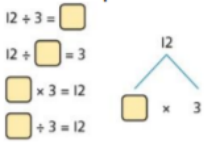
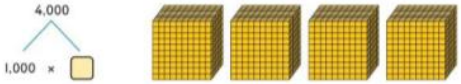
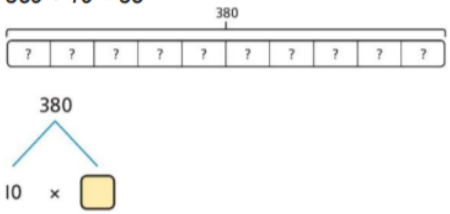
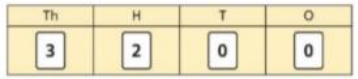
Dividing 2-digit and 3-digit numbers by a single digit by partitioning into 100s, 10s and 1s	Partition into 10s and 1s to divide where appropriate. *39 ÷ 3 = ?*  *39 = 30 + 9* *30 ÷ 3 = 10* *9 ÷ 3 = 3* *39 ÷ 3 = 13*	Partition into 100s, 10s and 1s using Base 10 equipment to divide where appropriate. *39 ÷ 3 = ?*  *39 = 30 + 9* *30 ÷ 3 = 10* *9 ÷ 3 = 3* *39 ÷ 3 = 13*	Partition into 100s, 10s and 1s using a part-whole model to divide where appropriate. *142 ÷ 2 = ?*  *100 ÷ 2 = 50* *40 ÷ 2 = 20* *6 ÷ 2 = 3* *50 + 20 + 3 = 73* *142 ÷ 2 = 73* **6. TO ÷ O Formal method with chunking** • TO ÷ O (with no remainders)  The chunking method is introduced but only with a single digit divisor. The number of groups should be recorded alongside on the right with the answer written on top of the bus stop. • TO ÷ O (with remainders)  The same layout is then used again but with remainders.

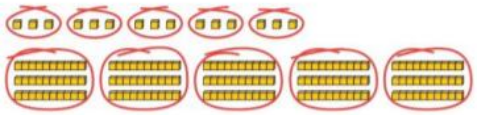
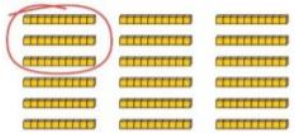
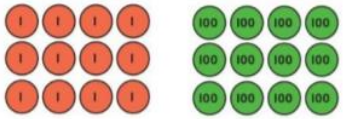
Year 5 Division

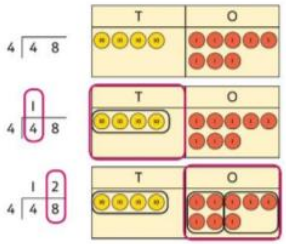
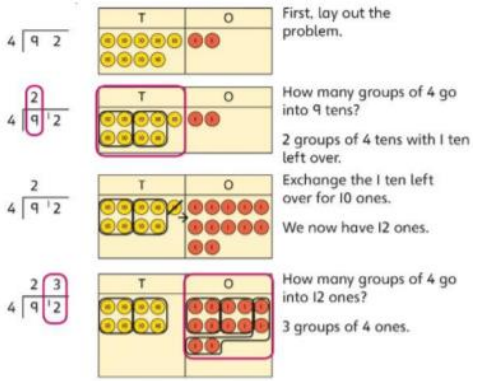
Pupils should be taught to:

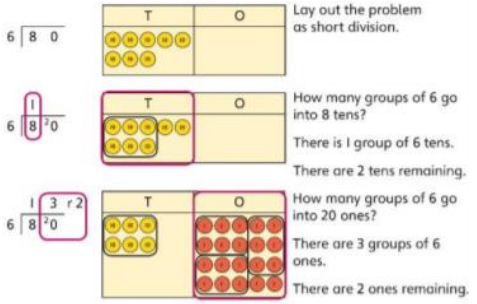
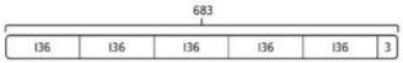
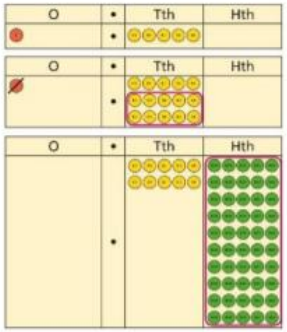
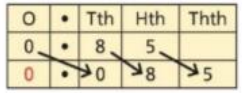
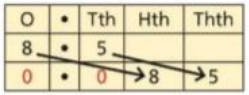
- divide numbers mentally, drawing upon known facts
- divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context
- divide whole numbers and those involving decimals by 10, 100 and 1,000
- solve problems involving division, including using their knowledge of factors and multiples squares and cubes
- solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign
- solve problems involving division, including scaling by simple fractions and problems involving simple rates

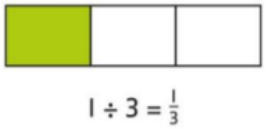
Understanding factors and prime numbers	Use equipment to explore the factors of a given number.  *24 ÷ 3 = 8* *24 ÷ 8 = 3* *8 and 3 are factors of 24 because they divide 24 exactly.*  *5 is not a factor of 24 because there is a remainder.*	Understand that prime numbers are numbers with exactly two factors. *13 ÷ 1 = 13* *13 ÷ 2 = 6 r 1* *13 ÷ 4 = 4 r 1* *1 and 13 are the only factors of 13.* *13 is a prime number.*	Understand how to recognise prime and composite numbers. *I know that 31 is a prime number because it can be divided by only 1 and itself without leaving a remainder.* *I know that 33 is not a prime number as it can be divided by 1, 3, 11 and 33.* *I know that 1 is not a prime number, as it has only 1 factor.*

Understanding inverse operations and the link with multiplication, grouping and sharing	Use equipment to group and share and to explore the calculations that are present. *I have 28 counters.* *I made 7 groups of 4. There are 28 in total.* *I have 28 in total. I shared them equally into 7 groups. There are 4 in each group.* *I have 28 in total. I made groups of 4. There are 7 equal groups.*	Represent multiplicative relationships and explore the families of division facts.  *60 ÷ 4 = 15* *60 ÷ 15 = 4*	Represent the different multiplicative relationships to solve problems requiring inverse operations.  Understand missing number problems for division calculations and know how to solve them using inverse operations. *22 ÷ ? = 2* *22 ÷ 2 = ?* *? ÷ 2 = 22* *? ÷ 22 = 2*
Dividing whole numbers by 10, 100 and 1,000	Use place value equipment to support unitising for division. *4,000 ÷ 1,000*  *4,000 is 4 thousands.* *4 × 1,000= 4,000* *So, 4,000 ÷ 1,000 = 4*	Use a bar model to support dividing by unitising. *380 ÷ 10 = 38*  *380 is 38 tens.* *38 × 10 = 380* *10 × 38 = 380* *So, 380 ÷ 10 = 38*	Understand how and why the digits change on a place value grid when dividing by 10, 100 or 1,000.  *3,200 ÷ 100 = ?* *3,200 is 3 thousands and 2 hundreds.* *200 ÷ 100 = 2* *3,000 ÷ 100 = 30* *3,200 ÷ 100 = 32* *So, the digits will move two places to the right.*

Dividing by multiples of 10, 100 and 1,000	Use place value equipment to represent known facts and unitising.  *15 ones put into groups of 3 ones. There are 5 groups.* *15 ÷ 3 = 5* *15 tens put into groups of 3 tens. There are 5 groups.* *150 ÷ 30 = 5*	Represent related facts with place value equipment when dividing by unitising.  *180 is 18 tens.* *18 tens divided into groups of 3 tens. There are 6 groups.* *180 ÷ 30 = 6*  *12 ones divided into groups of 4. There are 3 groups.* *12 hundreds divided into groups of 4 hundreds. There are 3 groups.* *1200 ÷ 400 = 3*	Reason from known facts, based on understanding of unitising. Use knowledge of the inverse relationship to check. *3,000 ÷ 5 = 600* *3,000 ÷ 50 = 60* *3,000 ÷ 500 = 6* *5 × 600 = 3,000* *50 × 60 = 3,000* *500 × 6 = 3,000*

Dividing up to four digits by a single digit using short division	Explore grouping using place value equipment. *268 ÷ 2 = ?* *There is 1 group of 2 hundreds.* *There are 3 groups of 2 tens.* *There are 4 groups of 2 ones.* *264 ÷ 2 = 134*	Use place value equipment on a place value grid alongside short division. The model uses grouping. A sharing model can also be used, although the model would need adapting.  Lay out the problem as a short division. *There is 1 group of 4 in 4 tens.* *There are 2 groups of 4 in 8 ones.* Work with divisions that require exchange.  	Use short division for up to 4-digit numbers divided by a single digit. $$7 \overline{)\,3\,{}^{3}8\,{}^{3}9\,{}^{4}2} \quad 0\;5\;5\;6$$ *3,892 ÷ 7 = 556* Use multiplication to check. *556 × 7 = ?* *6 × 7 = 42* *50 × 7 = 350* *500 × 7 = 3500* *3,500 + 350 + 42 = 3,892*

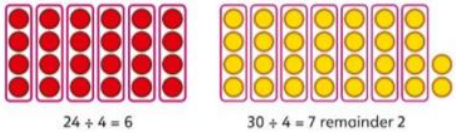
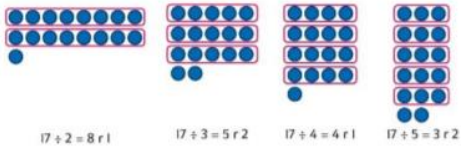
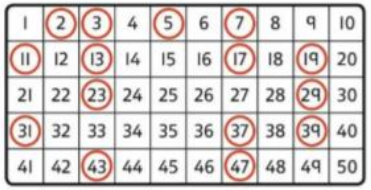
Understanding remainders	Understand remainders using concrete versions of a problem. *80 cakes divided into trays of 6.*  *80 cakes in total. They make 13 groups of 6, with 2 remaining.*	Use short division and understand remainders as the last remaining 1s. 	In problem solving contexts, represent divisions including remainders with a bar model.  *683 = 136 × 5 + 3* *683 ÷ 5 = 136 r 3*
Dividing decimals by 10, 100 and 1,000	Understand division by 10 using exchange. *2 ones are 20 tenths.* *20 tenths divided by 10 is 2 tenths.*	Represent division using exchange on a place value grid.  *1·5 is 1 one and 5 tenths.* *This is equivalent to 10 tenths and 50 hundredths.* *10 tenths divided by 10 is 1 tenth.* *50 hundredths divided by 10 is 5 hundredths.* *1·5 divided by 10 is 1 tenth and 5 hundredths.* *1·5 ÷ 10 = 0.15*	Understand the movement of digits on a place value grid.  *0·85 ÷ 10 = 0·085*  *8·5 ÷ 100 = 0·085*

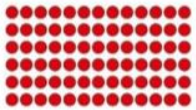
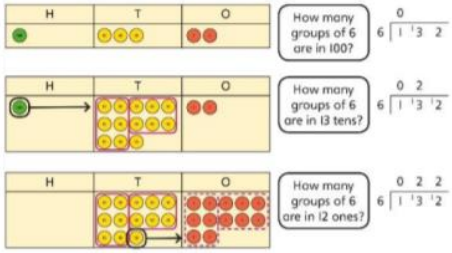
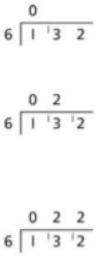
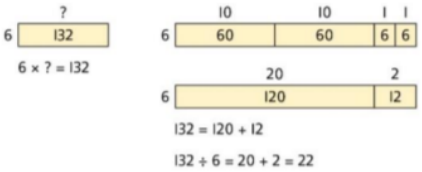
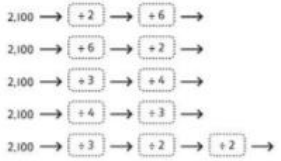
Understanding the relationship between fractions and division	Use sharing to explore the link between fractions and division. *1 whole shared between 3 people.* *Each person receives one-third.* 	Use a bar model and other fraction representations to show the link between fractions and division.  $1 \div 3 = \frac{1}{3}$	Use the link between division and fractions to calculate divisions. $5 \div 4 = \frac{5}{4} = 1\frac{1}{4}$ $11 \div 4 = \frac{11}{4} = 2\frac{3}{4}$

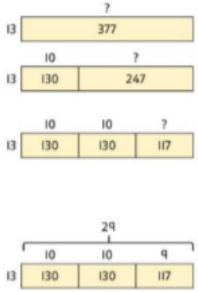
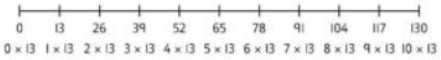
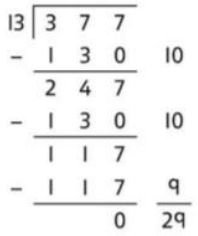
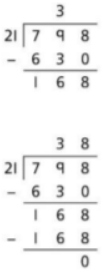
Year 6 Division

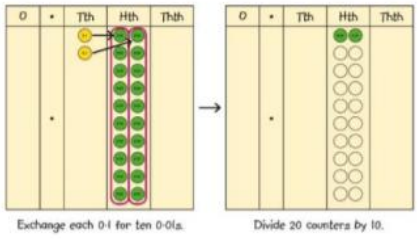
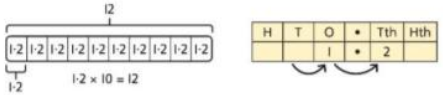
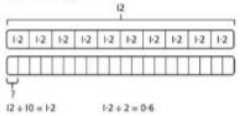
Pupils should be taught to:

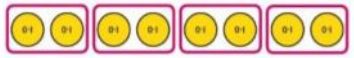
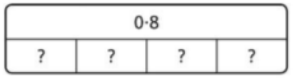
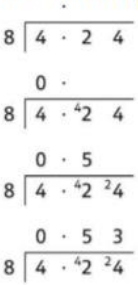
- divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context
- divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context
- perform mental calculations, including with mixed operations and large numbers
- use their knowledge of the order of operations to carry out calculations involving the 4 operations

Understanding factors	Use equipment to explore different factors of a number.  24 ÷ 4 = 6 30 ÷ 4 = 7 remainder 2 *4 is a factor of 24 but is not a factor of 30.*	Recognise prime numbers as numbers having exactly two factors. Understand the link with division and remainders.  17 ÷ 2 = 8 r 1 17 ÷ 3 = 5 r 2 17 ÷ 4 = 4 r 1 17 ÷ 5 = 3 r 2	Recognise and know primes up to 100. Understand that 2 is the only even prime, and that 1 is not a prime number. 

Dividing by a single digit	Use equipment to make groups from a total.  *There are 78 in total.* *There are 6 groups of 13.* *There are 13 groups of 6.*		Use short division to divide by a single digit.  Use an area model to link multiplication and division. 
Dividing by a 2-digit number using factors	Understand that division by factors can be used when dividing by a number that is not prime.	Use factors and repeated division. *1,260 ÷ 14 = ?*  *1,260 ÷ 2 = 630* *630 ÷ 7 = 90* *1,260 ÷ 14 = 90*	Use factors and repeated division where appropriate. *2,100 ÷ 12 = ?* 

Dividing by a 2-digit number using long division	Use equipment to build numbers from groups.  *182 divided into groups of 13.* *There are 14 groups.*	Use an area model alongside written division to model the process. *377 ÷ 13 = ?*  *377 ÷ 13 = 29*	Use long division where factors are not useful (for example, when dividing by a 2-digit prime number). Write the required multiples to support the division process. *377 ÷ 13 = ?*   *377 ÷ 13 = 29* A slightly different layout may be used, with the division completed above rather than at the side.  Divisions with a remainder explored in problem-solving contexts.

			8. Chunking (÷ 2 digits) • HTO ÷ TO (without remainders) 4 3 2 ÷ 1 6 = 2 7 The formal chunking method is reintroduced with a two digit divisor. • HTO ÷ TO (with remainders) 3 2 7 ÷ 1 9
Dividing by 10, 100 and 1,000	Use place value equipment to explore division as exchange.  Exchange each 0·1 for ten 0·01s. Divide 20 counters by 10. *0·2 is 2 tenths.* *2 tenths is equivalent to 20 hundredths.* *20 hundredths divided by 10 is 2 hundredths.*	Represent division to show the relationship with multiplication. Understand the effect of dividing by 10, 100 and 1,000 on the digits on a place value grid.  Understand how to divide using division by 10, 100 and 1,000. *12 ÷ 20 = ?*  	Use knowledge of factors to divide by multiples of 10, 100 and 1,000. 40 ÷ 50 = □ 40 → ÷ 10 → ÷ 5 → ? 40 → ÷ 5 → ÷ 10 → ? *40 ÷ 5 = 8* *8 ÷ 10 = 0·8* *So, 40 ÷ 50 = 0·8*

Dividing decimals	Use place value equipment to explore division of decimals.  *8 tenths divided into 4 groups. 2 tenths in each group.*	Use a bar model to represent divisions.  0·8 ? ? ? ? $4 \times 2 = 8$ $8 \div 4 = 2$ So, $4 \times 0{\cdot}2 = 0{\cdot}8$ $0{\cdot}8 \div 4 = 0{\cdot}2$	Use short division to divide decimals with up to 2 decimal places.  8 | 4 · 2 4 0 · 8 | 4 · $^{4}2$ 4 0 · 5 8 | 4 · $^{4}2$ $^{2}4$ 0 · 5 3 8 | 4 · $^{4}2$ $^{2}4$

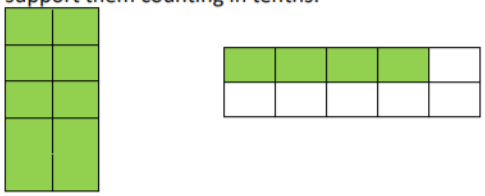
Year 3 Fractions

Pupils should be taught to:

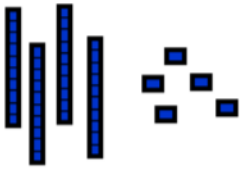
- count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit number or quantities by 10.
- recognise, find and write fractions of a discrete set of objects, unit fractions and non-unit fractions with small denominators
- recognise and use fractions as numbers, unit fractions and non-unit fractions with small denominators
- recognise and show, using diagrams, equivalent fractions with small denominators
- add and subtract fractions with the same denominator within one whole for example, 5/7 + 1/7 = 6/7
- compare and order unit fractions, and fractions with the same denominators
- solve problems that involve all of the above.

Counting in tenths

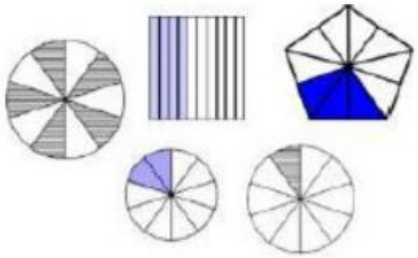
Children could use multiple tens frames to support them counting in tenths.



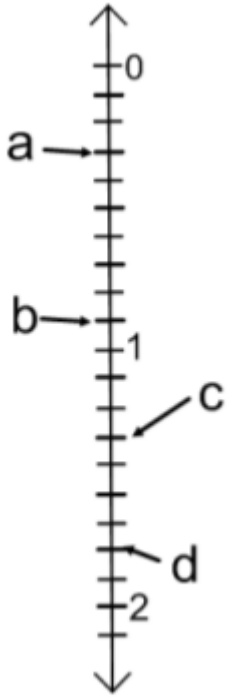
The children could use counters or shading. It is important that they can use the tens frame in different orientations.

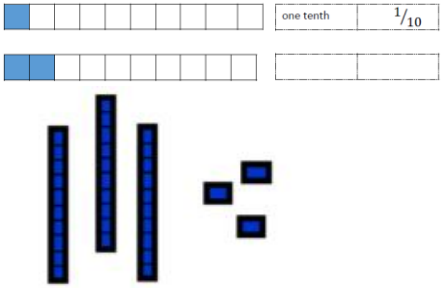


To start with, use the tenths cubes to embed the idea that 10 tenths = 1 whole. Children can then exchange their ten tenths for a 1 whole stick. Start at different points to rehearse counting forwards and backwards.

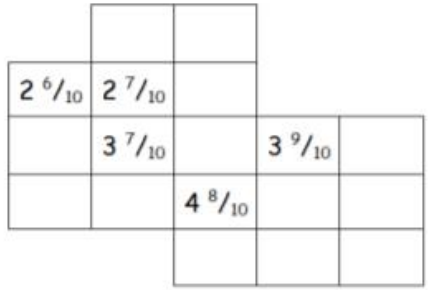


What does each image represent?
How many more sections would I need to shade to make $2\frac{7}{10}$?

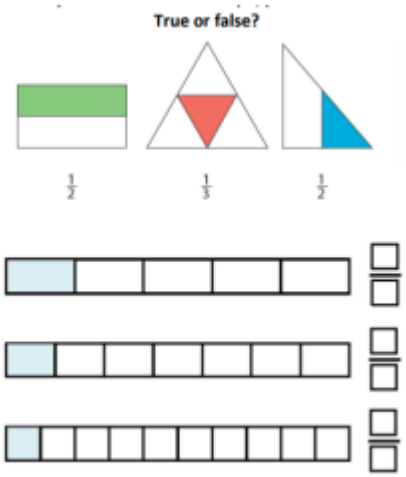
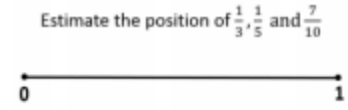


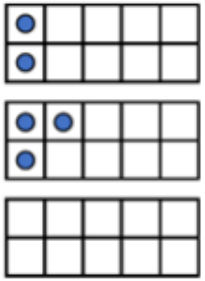
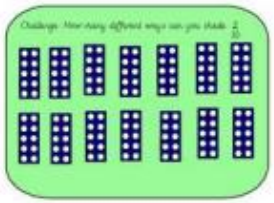
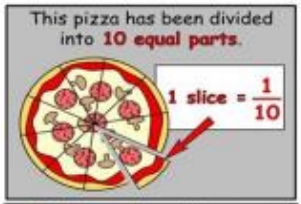
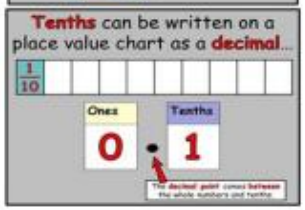
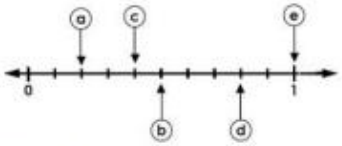
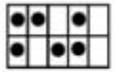


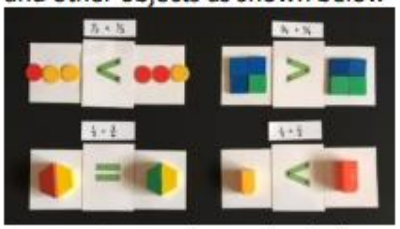
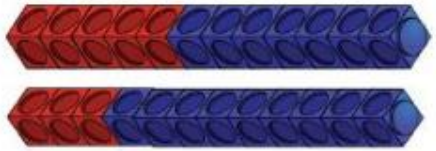
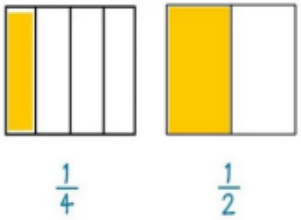
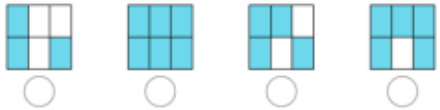
Sam started counting at $2\frac{7}{10}$. He finished with the picture above. How many tenths has he counted on?
Ext: This is Sam's finished image. Where could he have started counting? How many tenths away from this is it?

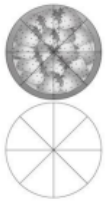
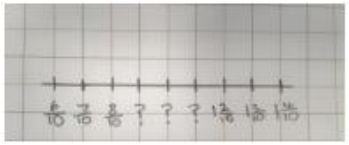
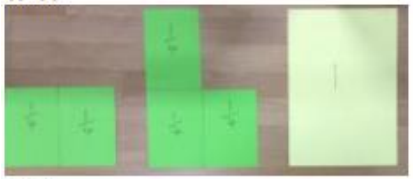
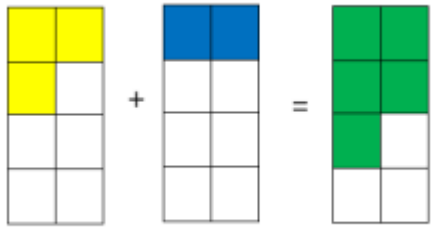
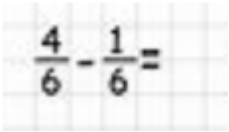


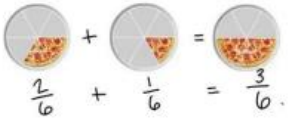
Here is part of a number square. Fill in the missing numbers.
(N.B. to extend more able learners, you may wish to remove $3\frac{9}{10}$ or extend the table beyond a whole.)

Identify fraction of shaded shape; position fractions on a number line; use fraction cards to show equivalence and compare fractions			 Continue the pattern. What do you notice? What about $^{1}/_{10}$ of 20? Use this to work out $^{2}/_{10}$ of 20, etc. True or false? $^{2}/_{10}$ of 20cm = 2cm $^{4}/_{10}$ of 40cm = 4cm $^{3}/_{5}$ of 20cm = 12cm

Recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10	 Use tens frames to represent tenths and count in tenths. Could also use a ten piece from numicon set with an object into the circles to represent the amount of tenths. Using 10p coins with 10 adding up to £1 - also links to the decimal place.  How many tenths of a whole pound do you have? 3/10 link to how it would be written as money £0.30.	    Which tenth is represented by the letter a? B? C? D? E? Eight tenths 7/10  8/10  6/10	**What do you notice?** $^{1}/_{10}$ of 10 = 1 $^{2}/_{10}$ of 10 = 2 $^{3}/_{10}$ of 10 = 3 Continue the pattern. **What do you notice?** What about $^{1}/_{10}$ of 20? Use this to work out $^{2}/_{10}$ of 20, etc. $^{1}/_{10}$ of 100 = 10 $^{1}/_{100}$ of 100 = 1 $^{2}/_{10}$ of 100 = 20 $^{2}/_{100}$ of 100 = 2 **How can you use this to work out $^{6}/_{10}$ of 200? $^{6}/_{100}$ of 200?** 

Compare and order unit fractions, and fractions with the same denominators	Equipment that could be used: Paper strips; Counters; Cubes; Fraction tiles; Fraction rods; Cuisenaire rods E.g. Compare fractions using counters and other objects as shown below  Paper strips can be used to help compare fractions. Ensure that the paper strips are of equal size.   Use cube towers to compare fractions.	This could begin by using paper strips before exposing children to pictorial representations such as:  $\frac{1}{4}$ $\frac{1}{2}$ $\frac{3}{8}$  $\frac{5}{8}$  $\frac{7}{8}$  Order the fractions in each row from smallest to largest. Use 1 for the smallest and 4 for the largest fraction. 	For example: Compare using =, < or > $^1/_2$, $^1/_5$, $^1/_3$, $^3/_4$ Compare using =, < or > $^2/_7$, $^5/_7$, $^4/_8$, $^5/_8$ 1 2 3 4 4 $\frac{1}{4} < \frac{B}{C}$ Order the following fractions from smallest to largest:

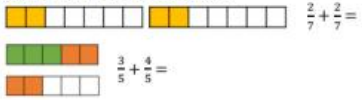
Add and subtract fractions with the same denominator within one whole	 Provide pupils with a strawberry tart cut into eighths and an identically sized and cut blank copy. *Collins Shanghai Y3 Unit 8.4* Determine that each part represents one eighth of the tart because the whole has been divided into eight equal parts. Get the children to cut out each part of the pie and label them as $\frac{1}{8}$. Hold up one piece in each hand and elicit that this is $\frac{2}{8}$. Record the calculation: $\frac{1}{8}+\frac{1}{8}=\frac{2}{8}$. Relate the common denominators to the number of equal pieces of the tart, and then discuss how by adding two of them together they get $\frac{2}{8}$. Ask what would happen if one more eighth was added to the new strawberry tart. Stick another eighth on to get $\frac{3}{8}$. Continue this process. Put the final piece on and remind the children that $\frac{8}{8}$ is the same as one whole (strawberry tart).	Count up and down in fraction amounts on a number line.  *Twinkl* Count up in fraction amounts using paper cards.  *I See*  	Make sure the numerators are the same, then add the denominators. e.g. $\frac{3}{8}+\frac{2}{8}=\frac{5}{8}$ 



When using numicon, the base piece represents the denominator and the top pieces represent the numerator. Cubes or pegs could also be used to represent the numerators.

Cube towers can be used:

Use the models to add the fractions:



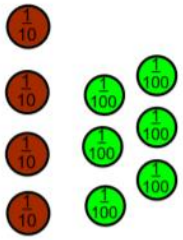
Similar resources can also be used to demonstrate subtraction of fractions.

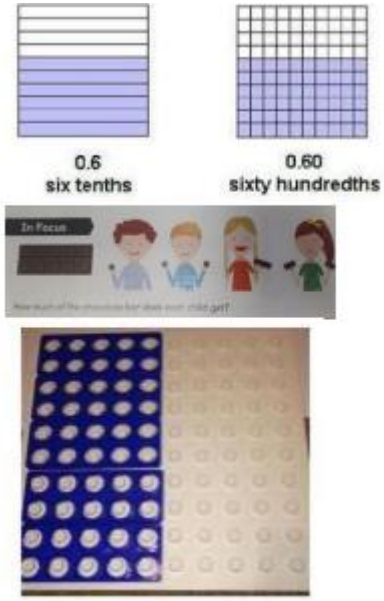
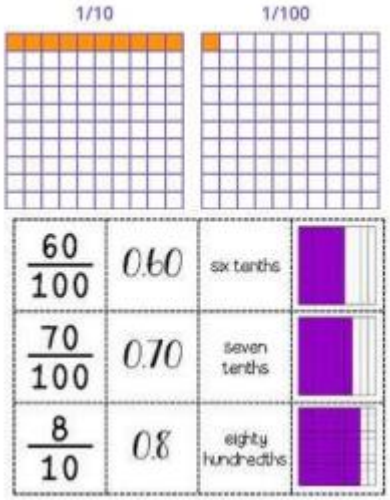
Year 4 Fractions

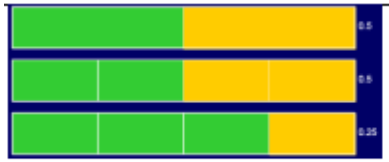
Pupils should be taught to:

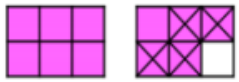
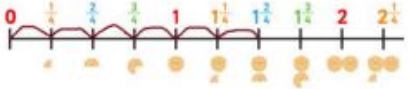
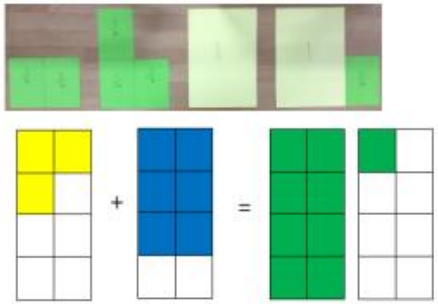
- recognise and show, using diagrams, families of common equivalent fractions
- count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten.
- solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number
- add and subtract fractions with the same denominator
- recognise and write decimal equivalents of any number of tenths or hundredths
- recognise and write decimal equivalents to 1/4 , 1/2 , 3/4
- find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths
- round decimals with one decimal place to the nearest whole number

- compare numbers with the same number of decimal places up to two decimal places
- solve simple measure and money problems involving fractions and decimals to two decimal places.

Counting up and down in hundredths.	Use 100 bead strings to rehearse counting forwards and backwards. Use different starting points and draw discussion into the fact that $^{1}/_{10} = {}^{10}/_{100}$.  To start with, use the hundredths counters to embed the idea that 10 hundredths = 1 tenth. Children can then exchange their ten hundredths for a tenth counter. Start at different points to rehearse counting forwards and backwards.	As for counting in tenths Use dienes units blocks to represent 1/100 Use pennies to recognise 1/100 of a pound etc Decimal Number Chart 0.01-1 0.01 0.02 0.03 0.04 0.05 0.06 0.07 0.08 0.09 0.1 0.11 0.12 0.13 0.14 0.15 0.16 0.17 0.18 0.19 0.2 0.21 0.22 0.23 0.24 0.25 0.26 0.27 0.28 0.29 0.3 0.31 0.32 0.33 0.34 0.35 0.36 0.37 0.38 0.39 0.4 0.41 0.42 0.43 0.44 0.45 0.46 0.47 0.48 0.49 0.5 0.51 0.52 0.53 0.54 0.55 0.56 0.57 0.58 0.59 0.6 0.61 0.62 0.63 0.64 0.65 0.66 0.67 0.68 0.69 0.7 0.71 0.72 0.73 0.74 0.75 0.76 0.77 0.78 0.79 0.8 0.81 0.82 0.83 0.84 0.85 0.86 0.87 0.88 0.89 0.9 0.91 0.92 0.93 0.94 0.95 0.96 0.97 0.98 0.99 1	As for counting in tenths 9.8 is equivalent to 980 hundredths, 9.82 is equivalent to ? hundredths. How many hundredths are there in 10.0? Using a partially filled in hundredths square, ask how you know where e.g. 2.76 would go. 2.52 | 2.53 | | | | | | | | | | | 2.67 | | | | | | | 2.82 | | | 2.85 | 2.86 | | | | | | 2.96 | |

Recognise and write decimal equivalents of any number of tenths or hundredths			**What do you notice?** One tenth of £41 One hundredth of £41 One thousandth of £41 Continue the pattern. What do you notice? 0.085 + 0.015 = 0.1 0.075 + 0.025 = 0.1 0.065 + 0.035 = 0.1 Continue the pattern for the next five number sentences

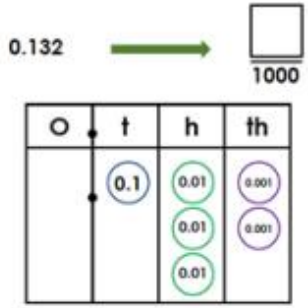
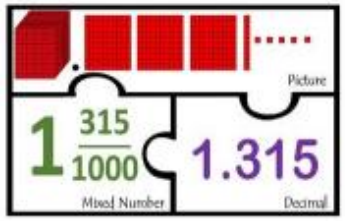
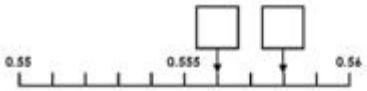
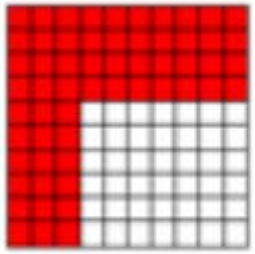
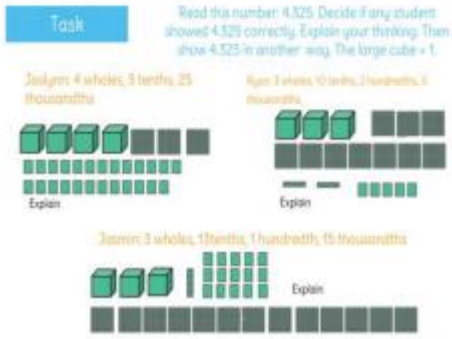
Recognise and write decimal equivalents to ¼ , ½, ¾		 Explore using link: https://mathsframe.co.uk/en/resources/resource/66/itp-fractions 	Match each fraction to its decimal equivalent. $\frac{1}{2}$ $\frac{4}{10}$ $\frac{3}{4}$ $\frac{1}{4}$ 0·25 0·75 0·4 0·5 Circle the equivalent fraction to 0·25. $\frac{2}{5}$ $\frac{5}{2}$ $\frac{25}{100}$ $\frac{100}{25}$ Round to the nearest whole number. $8\frac{3}{8}$ 8·38 8·83 Using these cards can you make a number between 4·1 and 4·61? 1 4 6 · What is the smallest number you can make using all four cards? What is the largest number you can make using all four cards?

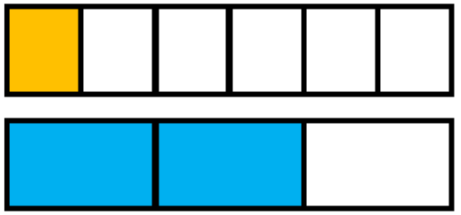
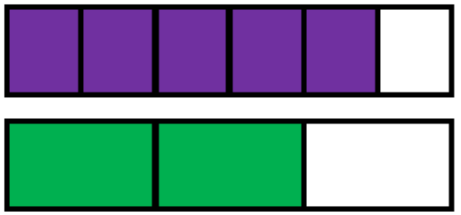
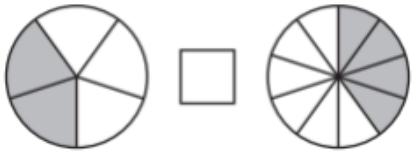
Add and subtract fractions with the same denominator including bridging over whole numbers e.g. $7/9 + 4/9 = 11/9$ or 1 whole and $2/9$	As before, use cubes and numicon to create the fractions:  $\frac{11}{6} - \frac{\square}{6} = \frac{\square}{6}$	Count up and down in fraction amounts on a number line.  *Twinkl* Count up in fraction amounts using paper cards. *I See* 	Make sure the numerators are the same, then add the denominators. If your answer is an improper fraction, convert it to a mixed number if the problem requires it. e.g. $\frac{7}{9} + \frac{4}{9} = \frac{11}{9}$ or $1\frac{2}{9}$

Year 5 Fractions

Pupils should be taught to:

- compare and order fractions whose denominators are all multiples of the same numbers
- identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths
- recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number [for example, 5 2 + 5 4 = 5 6 = 1 5 1]
- add and subtract fractions with the same denominator and denominators that are multiples of the same number
- multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams read and write decimal numbers as fractions [for example, 0.71 = 100 71]
- recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents
- round decimals with two decimal places to the nearest whole number and to one decimal place
- read, write, order and compare numbers with up to three decimal places
- solve problems involving number up to three decimal places
- recognise the percent symbol (%) and understand that per cent relates to 'number of parts per hundred', and write percentages as a fraction with denominator 100, and as a decimal
- solve problems which require knowing percentage and decimal equivalents of 1/2 , 1/4 , 1/5 , 2/5 , 4/5 and those fractions with a denominator of a multiple of 10 or 25.

Recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents	 Use place value counters and grid to represent decimal numbers up to three decimal points and convert to fractions  Using base ten to physically represent decimal numbers.	 Use number lines to represent thousandths as the steps between hundredths.  Using a tens frame, 100 square, or thousands grid to represent tenths, hundredths and thousandths 	One tenth of £41 One hundredth of £41 One thousandth of £41 Continue the pattern What do you notice? 0.085 + 0.015 = 0.1 0.075 + 0.025 = 0.1 0.065 + 0.035 = 0.1 Continue the pattern for the next five number sentences. One thousandth of my money is 31p. How much do I have? True or false? 0.1 of a kilometre is 1m. 0.2 of 2 kilometres is 2m. 0.3 of 3 kilometres is 3m 0.25 of 3m is 500cm. $^{2}/_{5}$ of £2 is 20p True or false? 25% of 23km is longer than 0.2 of 20km. Convince me.

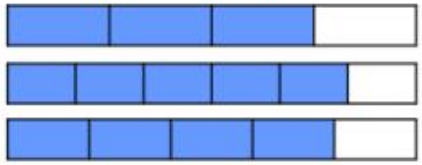
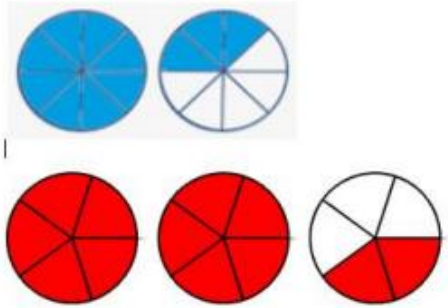
Compare and order fractions whose denominators are all multiples of the same number	 Fraction tiles can be laid out to compare different sized fractions. 	 or  	For example: Order the following fractions from smallest to largest: $^{2}/_{3}, ^{3}/_{4}, ^{2}/_{6}, ^{1}/_{12}, ^{5}/_{6}$ Which is larger; $^{5}/_{8}$ or $^{3}/_{4}$ Using the number cards, can you complete the equation. Can you find more than one possibility? $\frac{7}{11} < \square\square < \frac{8}{11}$ 11 15 22 25 33

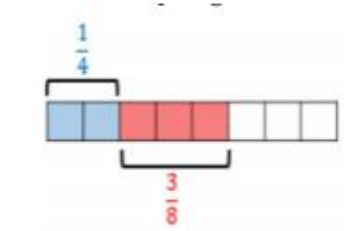
Add and subtract fractions with different denominators where one denominator is a multiple of the another within the calculation	$\frac{3}{8} + \frac{1}{4} = \frac{3}{8} + \frac{2}{8} =$  Using paper strips, create fractions where one denominator is a multiple of the other and demonstrate how to convert one denominator into the other by splitting the fraction, so the denominators are equal.	$\frac{1}{3} - \frac{1}{12} =$  $\frac{1}{3} + \frac{5}{6} =$ 	$\frac{2}{5} - \frac{1}{10} = \frac{4}{10} - \frac{1}{10} = \frac{3}{10}$

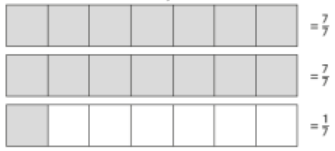
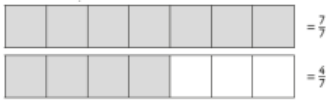
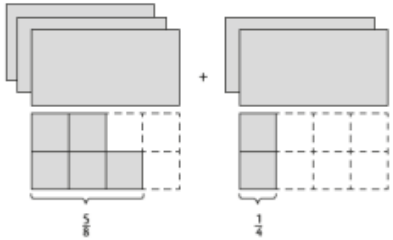
Year 6 Fractions

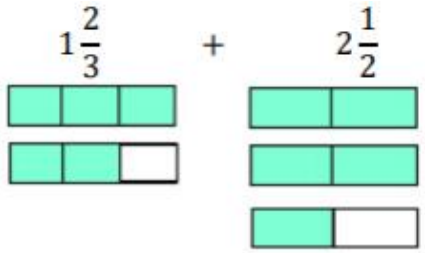
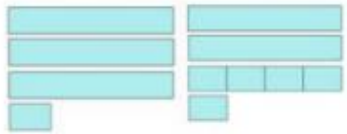
Pupils should be taught to:

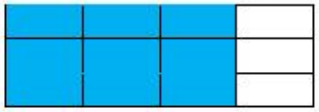
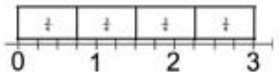
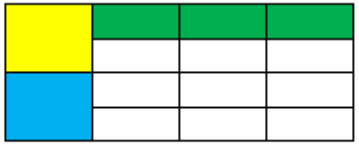
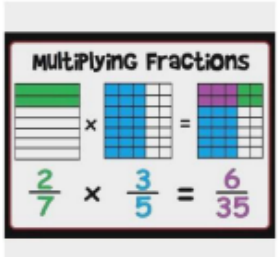
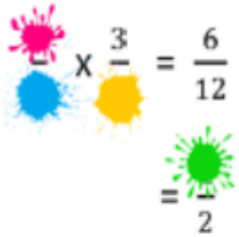
- use common factors to simplify fractions; use common multiples to express fractions in the same denomination
- compare and order fractions, including fractions > 1
- add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions
- multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, 4 1 × 2 1 = 8 1]
- divide proper fractions by whole numbers [for example, 3 1 ÷ 2 = 6 1]
- associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction [for example, 3/8]
- identify the value of each digit in numbers given to three decimal places and multiply and divide numbers by 10, 100 and 1000 giving answers up to three decimal places
- multiply one-digit numbers with up to two decimal places by whole numbers
- use written division methods in cases where the answer has up to two decimal places
- solve problems which require answers to be rounded to specified degrees of accuracy
- recall and use equivalences between simple fractions, decimals and percentages, including in different contexts.

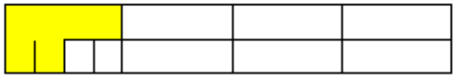
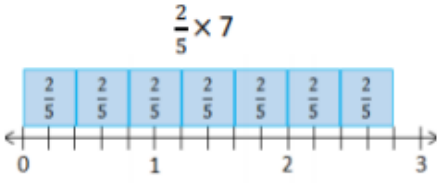
Compare and order fractions, including fractions >1	  Building on to: Which is greater?	Order the fractions represented by the bar models in descending order:  Compare the fractions below. Explain which is larger and how you can prove it. 	Order the fractions below in descending order: $\frac{5}{6}$ $\frac{1}{4}$ $\frac{3}{10}$ $\frac{2}{5}$ $\frac{1}{2}$ Use < > or = to make the statement correct: $1\frac{2}{7} \bigcirc 1\frac{4}{5}$ $\frac{4}{\square} > \frac{3}{4}$ $\frac{\square}{4} < \frac{2}{5}$ $\frac{4}{\square} = \frac{1}{2}$ Can you use the digit cards to make the statement true using improper fractions 16 50 24 51 $\frac{\square}{\square} < \frac{\square}{\square}$

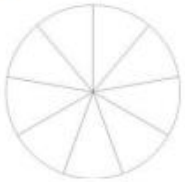
Add and subtract fractions with different denominators	Once they have combined their previous knowledge of +/- fractions with their knowledge of equivalent fractions, the process is as above.	 $\frac{1}{2}+\frac{1}{8}=\frac{4}{8}+\frac{1}{8}=\frac{5}{8}$  $\frac{1}{4}+\frac{3}{8}=\frac{2}{8}+\frac{3}{8}=\frac{5}{8}$ 	$\frac{3}{4}+\frac{2}{5}=\frac{15}{20}+\frac{8}{20}=\frac{23}{20}$ or $1\frac{3}{20}$ $\frac{3}{4}+\frac{2}{5}=\frac{15}{20}+\frac{8}{20}=\frac{23}{20}$ or $1\frac{3}{20}$

Add and subtract fractions, including mixed numbers and improper fractions where the no bridging is required	**Addition** Provide pupils with strips split into sevenths. Elicit that $\frac{15}{7}$ is the same $2\frac{1}{7}$  Elicit that $\frac{11}{7}$ is the same $1\frac{4}{7}$  Question: How many sevenths do we have altogether? Twenty six sevenths. Reminder: when adding/subtracting two fractions, the denominator stays the same – even when it is an improper fraction. Elicit that $\frac{26}{7}$ is equivalent to $3\frac{5}{7}$ Use a similar example to model the same for subtraction.	Oscar was running a race. He ran $3\,^{5}/_{8}$ of a kilometre in the first 15 minutes. He ran $2\,^{1}/_{4}$ of a kilometre in the second 15 minutes. How far had he run in total after 30 minutes? Share the following image:  Elicit that one full sheet of paper represents 1km. Agree that he has run five full kilometres because there are five full sheets. Ask: Oscar ran further than 5 km. How much further? Agree that Oscar has also ran $\frac{5}{8}$ km and $\frac{1}{4}$ km. Establish that these are related fractions because one denominator is a multiple of the other. Share the following then get pupils to discuss what is happening: $3\frac{5}{8}+2\frac{1}{4}=3\frac{5}{8}+2\frac{2}{8}$ $=(3+\frac{5}{8})+(2+\frac{2}{8})$ $=(3+2)+(\frac{5}{8}+\frac{2}{8})$ $=(5+\frac{7}{8})$ $=5\frac{7}{8}$ *Collins Shanghai Y6 Unit 6.7* Use a similar example to model the same for subtraction.	$3\frac{3}{4}+\frac{1}{5}=3\frac{19}{20}$ $11\frac{3}{4}-7\frac{1}{6}=4\frac{7}{12}$

Add and subtract fractions, including mixed numbers and improper fractions where bridging is required	**Addition** Example: $3\frac{5}{7} + 2\frac{4}{7}$ Use the same method as previously with the strips, but get the children to cut up the fraction elements into the component sevenths. This would leave 5 wholes (5 strips of $\frac{7}{7}$) and nine $\frac{1}{7}$ parts. Elicit that nine $\frac{1}{7}$ parts is the same as $\frac{9}{7}$ or $1\frac{2}{7}$ parts. Combine 5 with $1\frac{2}{7}$ to get the answer of $6\frac{2}{7}$ **Subtraction** Example: $4\frac{2}{7} - 2\frac{5}{7}$ Use the same method as previously with the strips, but get the children to cut up the fraction elements into the component sevenths. This would leave 2 wholes (2 strips of $\frac{7}{7}$) but then they would realise that they cannot take $\frac{5}{7}$ away from $\frac{2}{7}$. Discuss what could be done next. Elicit that they could cut one of their two wholes into $\frac{7}{7}$. Going back to their original $4\frac{2}{7}$ they would the re-partition that into $3\frac{9}{7}$. With $3\frac{9}{7}$ in strips, they could remove the 2 wholes then the $\frac{4}{7}$ leaving them with $1\frac{5}{7}$.	  Calculate $3\frac{1}{4} - 1\frac{3}{4}$ $3\frac{1}{4}$ can become $2\frac{5}{4}$ 	For example $3\frac{3}{4} + \frac{7}{5} = 5\frac{3}{20}$ $11\frac{3}{4} - 7\frac{5}{6} = 3\frac{11}{12}$

Multiply simple pairs of proper fractions, writing the answer in its simplest form Multiply fractions by whole numbers	 Use Cuisenaire Rods and fraction towers to demonstrate multiplying fractions by an integer.  Using fraction towers to demonstrate the abstract: '3 lots of ¼ =' 2 lots of $^{2}/_{6}$ = Use bar models to work out 3 x ¾ =  Use a number line to work it out: 	Use a diagram to represent multiplying fractions. Build an array (as used when multiplying whole numbers For example ¼ x 2/4  Draw a bar and shade ¼ Draw an adjoining column and shade 2/4 . The shaded cells represent the total.(2/16 or 1/8) 	Solve: $\frac{2}{\square} \times \frac{\square}{\square} = \frac{6}{20} = \frac{\square}{\square}$ $\frac{\square}{\square} \times \frac{\square}{5} = \frac{10}{60} = \frac{\square}{\square}$ How many ways can you answer the following?  In each number sentence, replace the boxes with different whole numbers less than 20 so that the number sentence is true.

		Draw your own bar model to work out the following: 2 x 2/3 = 4 x 2/3 =  Find 2/4 of ¼ (2/4 x ¼)    	$\frac{1}{\square} \times \frac{3}{\square} = \frac{\square}{\square}$ $\frac{\square}{\square} \times \frac{\square}{\square} = \frac{8}{15}$ $\frac{2}{\square} \times \frac{5}{\square} < \frac{10}{\square}$ $\frac{\square}{\square} \div 3 = \frac{1}{\square}$ $\frac{\square}{\square} \div 3 > \frac{1}{4}$

Divide proper fraction by whole numbers.	Using paper strips is a good way to demonstrate what happens to a fraction when it is divided by a whole integer i.e. 2 Fold the paper in half: ***What happens when I divide $^{1}/_{2}$ by 2?*** By folding each half into two parts, it becomes clear that quarters have been formed.	Lee has $\frac{2}{5}$ of a chocolate bar. He shares it with his friend. How much chocolate do they get each?  Use the diagrams to help you calculate:  Calculate the following and use the diagram to help you. $\frac{1}{8} \div 4 =$ 	Solve: $6 \div \_\_ = 9$ $\_\_\_ \div \frac{2}{5} = 10$ $\_\_ \div \_\_\_ = 5\frac{5}{6}$ Harjoht's Mum ordered pizza for the whole family. Harjoht ate ¼ of the pizza. His Mum, brother and sister ate the rest of the pizza. What fraction of the pizza did they get each? Molly's Mum ordered pizza for the whole family. Molly ate ¼ of the pizza. Six members of the family eat the remaining pizza. What fraction of the pizza did they get each?

Vocabulary

Reception

Number: Counting and number properties		
backwards count / counting digit even forwards	none number numeral odd	one, two *up to and beyond* twenty pattern subitise zero
Number: Place value, ordering and comparing		
after before compare different end equal to in between less / less than	many middle more / more than nearer next not equal one less one more	order pattern same sort start
Number: Calculation		
add altogether difference double group	half left make part regroup	share take away total whole

Fractions		
double equal half	not equal part	share whole

Measurement: Mass		
heavier / heavier than heavy	light lighter / lighter than	weigh weight

Measurement: Length		
bigger longer shorter	smaller taller thinner	wider / fatter / thicker

Geometry: Properties of shapes		
circle pattern rectangle square	triangle	
Geometry: Position and direction		
above backwards below behind beside between down	forwards in next to on on top of over over	through turn turn around turn towards under up

Year 1

Number: Counting and number properties		
number	twenty-one	even
count / counting	twenty-two	pattern
forwards	twenty-three	steps of
backwards	twenty-four	multiple
count on	*up to*	subitise
countback	ninety-nine	
zero	odd	
Number: Place value, ordering and comparing		
value	first	below
digit	second	middle
same	third	sort
different	fourth	sequence
one / ones	fifth	
ten / tens	*up to*	
hundred	twentieth	
column	order	
one-digit	amount	
two-digit	size	
more / more than	number line	
less / less than	larger / largest	
fewer/ fewer than	bigger / biggest	
equal / equal to / =	smaller / smallest	
not equal	estimate	
most	compare	
fewest	between	
least	above	
Number: Calculation		
total / in total	missing number problems	lots of
sum	left / leftover	groups of
plus	part	times
add / addition / +	whole	array
altogether	unknown	regroup / regrouping
combine	number sentence	addend
number bond	equal	subtrahend
difference	equally	minuend
distance between	unequal	bar model
subtract / subtraction / -	pair	remainder
minus	group / grouped	multiple / multiples
take away / taken away	grouping	
how much	share / shared	
how many	sharing	
bonds	double / doubling / doubles	
start / change/ result	twice as	
facts	each	
problems	half / halving / halves	

Fractions		
half / halve / halves quarter / quarters one-quarter two-quarters three-quarters sharing group / groups	grouping part whole equal parts same size bar equal / equally	

Measurement: Time		
year month week day weekday weekend chronological order days of the week Monday Tuesday Wednesday Thursday Friday Saturday Sunday months of the year January February March April	May June July August September October November December night hour minute second morning afternoon evening yesterday today tomorrow before after	old / older new / newer clock / clock face o'clock half past birthday watch hour minute minutes past / to quarter past / to half past fast / faster /fastest quick / quicker / quickest slow / slower / slowest early earlier late later time
Measurement: Mass		
weigh weight heavy heavier / heavier than heaviest	light lighter / lighter than lightest balance (weighing) scales	ruler mass gram kilogram
Measurement: Length		
height long / longer / longest tall / taller / tallest short / shorter / shortest	wide / wider / widest narrow/ narrower/ narrowest centimetre metre	far distance measure

Measurement: Capacity		
volume full / fuller / fullest empty / emptier / emptiest	more than less than half full	half quarter capacity
Measurement: Money		
coin / coins note / notes amount penny / p pound / £	one penny two pence five pence ten pence twenty pence	fifty pence combination money

Geometry: Properties of shapes		
pattern 2-D rectangle / rectangles square / squares circle / circles kite / kites triangle / triangles 3-D cube / cubes cuboid / cuboids	pyramid / pyramids cylinder / cylinders sphere / spheres side / sides line straight curved flat open / closed shape corner	base point
Geometry: Position and direction		
left right top middle bottom	on top of in front of behind between	above below beneath around

Year 2

Number: Counting and number properties		
numeral hundreds	step counting	count in multiples
Number: Place value, ordering and comparing		
place value partition place holder estimate estimation	half-way three-digit equivalent greater than >
less than <	digit
Number: Calculation		
commutative inverse calculate multiplication division times tables multiplication table repeated addition	reordering mental method written method reduce increase combination multiply / multiplied fact family	calculation divide remainder multiple / multiples

Fractions		
two-quarters third one-third two-thirds equivalent / equivalence one whole one and a quarter	one and two-quarters one and a half one and three-quarters half as much twice as much numerator denominator	

Measurement: Time		
analogue quarter past / to five / ten / past / to	clockwise anticlockwise noon	midday midnight intervals of time
Measurement: Mass		
gram / g	kilogram / kg	scale
Measurement: Length		
height width metre / m	centimetre / cm scale standard units	

Measurement: Capacity		
litre / l millilitre / ml	scale quarter full	three-quarters full
Measurement: Money		
price cost	amount change	value
Measurement: Temperature		
temperature degrees	Celsius / °C thermometer	scale

Geometry: Properties of shapes		
vertical horizontal Vertex / vertices edge / edges face / faces quadrilateral / quadrilaterals polygon / polygons pentagon / pentagons	hexagon / hexagons heptagon / heptagons octagon / octagons prism / prisms cone / cones symmetry line of symmetry surface	mirror line properties classify opposite
Geometry: Position and direction		
sequence rotate rotation angle right angle	straight line arrange anticlockwise row column	

Statistics		
pictogram tally chart tallies block diagram table data category / categories	key sorting totalling comparing horizontal vertical	

Addition & Subtraction

Years 3 and 4: add, addition, more, plus, increase, sum, total, altogether, double, near double, how many more to make…? how many more to make…? how many more is… than…? how much more is…? -, subtract, subtraction, take (away), minus, decrease, leave, how many are left/left over? how many fewer is… than…? how much less is…? difference between, half, halve, how many more/fewer is… than…? how much more/less is…? Is equal to, is the same as, tens boundary, hundreds boundary, inverse

Years 5 and 6: add, addition, more, plus, increase, sum, total, altogether, double, near double, how many more to make…? subtract, subtraction, take (away), minus, decrease, leave, how many are left/left over? difference between, half, halve, how many more/fewer is… than…? how much more/less is…? Is equal to, sign, is the same as, tens boundary, hundreds boundary, units boundary, tenths boundary, inverse

Multiplication & Division

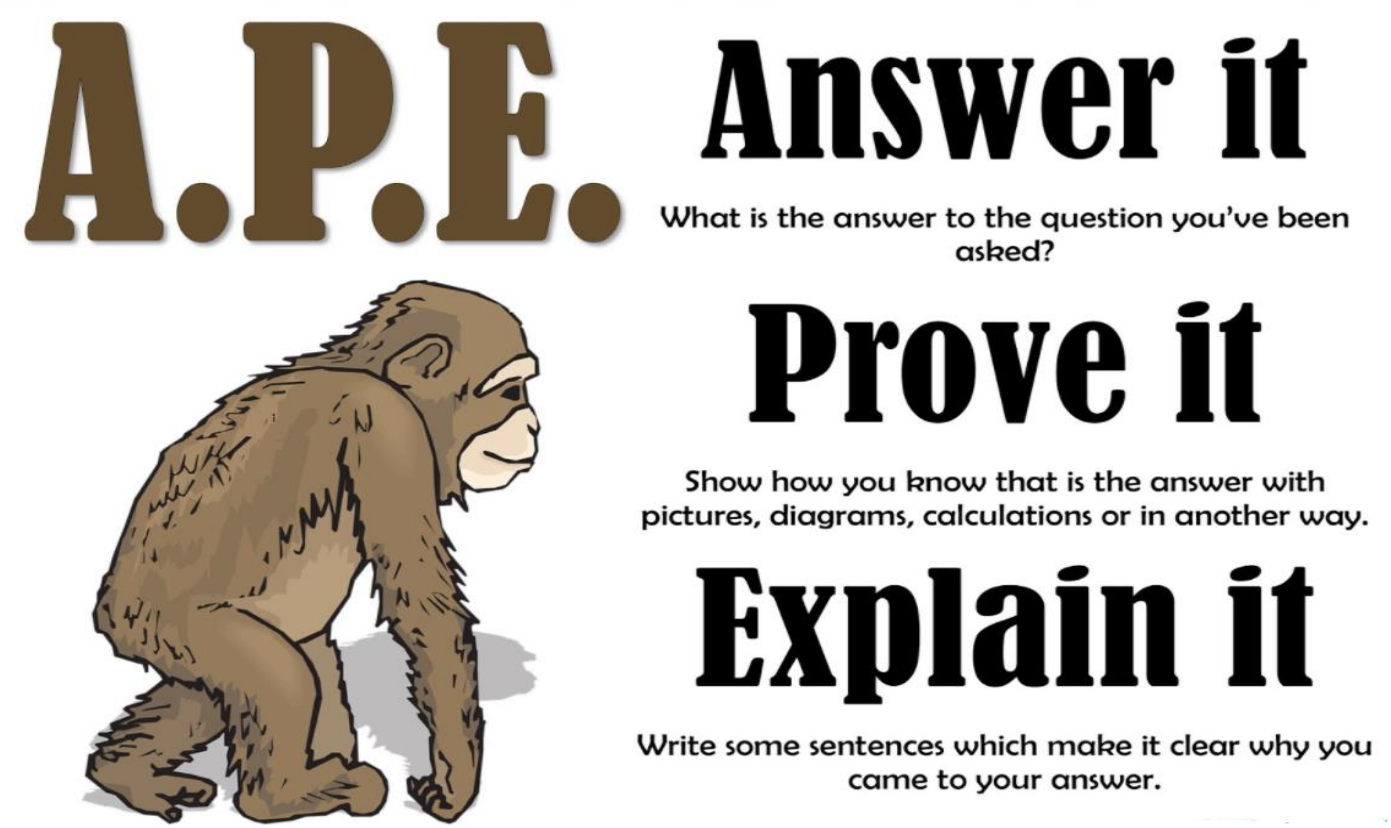
Year 3 and 4: lots of, groups of, times, multiply, multiplication, multiplied by, multiple of, product, once, twice, three times… ten times…times as (big, long, wide… and so on), repeated addition, array, row, column, double, halve, share, share equally, one each, two each, three each…group in pairs, threes… tens, equal groups of, divide, division, divided by, divided into, remainder, factor, quotient, divisible by, inverse

Years 5 and 6: lots of, groups of, times, multiply, multiplication, multiplied by, multiple of, product once, twice, three times… ten times…times as (big, long, wide… and so on), repeated addition array, row, column, double, halve, share, share equally, one each, two each, three each…group in pairs, threes… tens, equal groups of, divide, division, divided by, divided into, dividend, divisor, remainder, factor, quotient, divisible by, inverse, fraction

Reasoning and Problem Solving

All children to be given the opportunity to reason and problem solve at least once a week.

Children should be using the Answer Prove it Explain it guidelines when reasoning.



See Reasoning Examples for further guidance.